

Lignes d'ancrage en fibre synthétiques

De l'approche théorique à l'application pour des éoliennes offshore flottantes

Laure Civier

Ingénieure de recherche en ancrage innovants

I. France Energies Marines institute

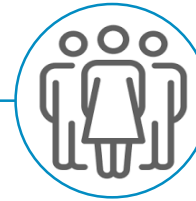
II. Industrial context

III. Behavior law for mooring design

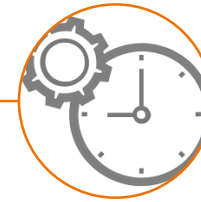
IV. Study of fatigue lifetime

V. Multi-scale modeling

Institut de recherche et
d'innovation
sur l'éolien en mer
reconnu pour son impact
industriel, économique et
sociétal



100 collaborateurs



Depuis 2012



10 M€ d'activité en 2024



Siège à **Brest**
Antennes au **Havre, Nantes et**
Marseille



ITE soutenu par les
le plan d'investissement
France 2030

Un partenariat public-privé

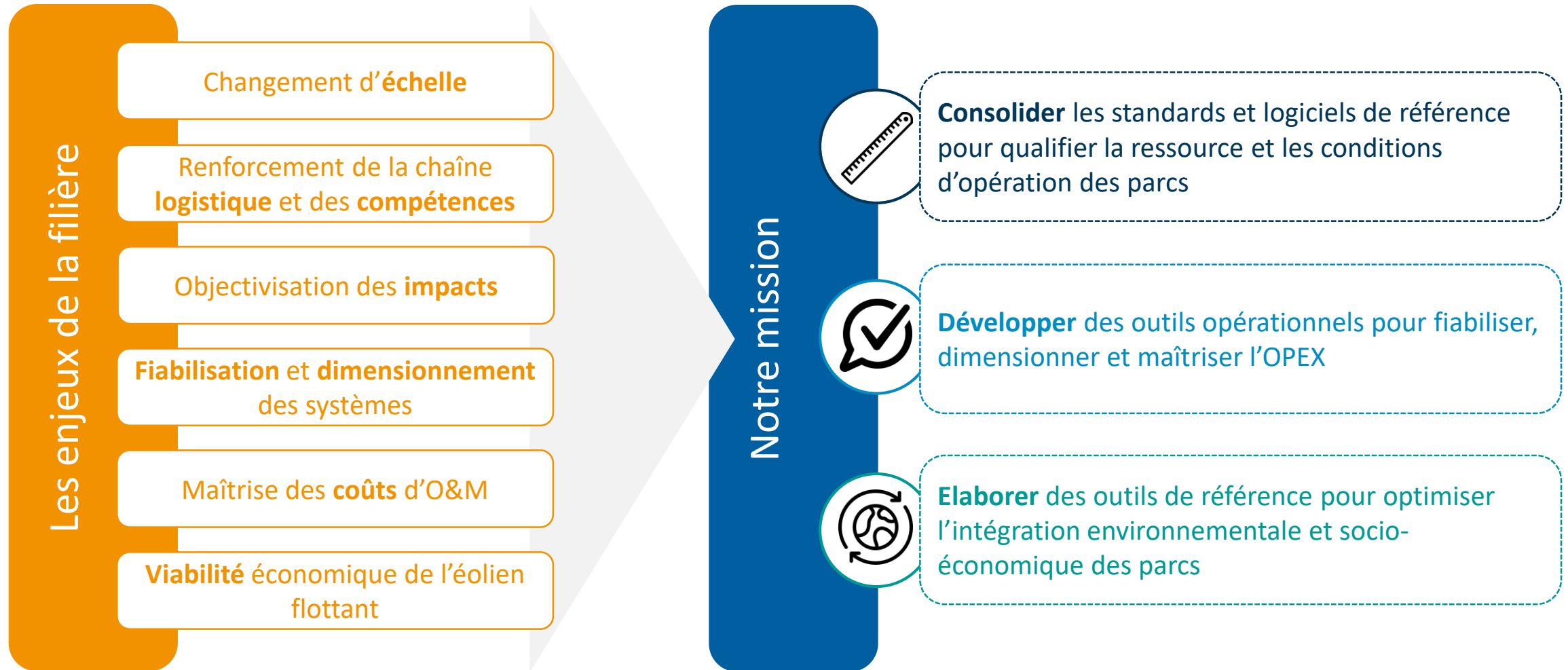


Actionnariat
50 % public
50 % privé



SAS avec
un capital de
699 000 €





CARACTÉRISATION DE SITES

- Spatialisation des observations
- Caractérisation des états de mer
- Caractérisation du vent en mer
- Changement climatique
- Processus hydrosédimentaires



DIMENSIONNEMENT ET SUIVI DES SYSTÈMES

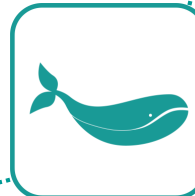
- Structure, ancrages et câble électrique
- Couplage hydrodynamique et structure
- Jumeaux numériques et suivi en service
- Innovation technologique



4 programmes de R&D transversaux et complémentaires

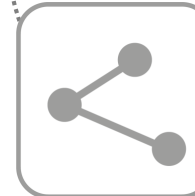
INTÉGRATION ENVIRONNEMENTALE

- Effets sur les compartiments de l'écosystème
- Changement d'échelle socio-écosystémique, spatiale et temporelle
- Outils pour l'intégration environnementale



OPTIMISATION DES PARCS

- Architecture de ferme
- Intégration aux réseaux (hydrogène...)
- Installation, opération et maintenance



Un comité scientifique & technologique indépendant



Deborah GREAVES



Caractérisation
de sites



Xiaoli GUO LARSÉN



Erin BACHYNSKI-POLIĆ



Dimensionnement et suivi des systèmes
Optimisation des parcs



Hannele HOLTINEN



Emmanuel BRANLARD



Thomas Michel SAUDER



THE UNIVERSITY of EDINBURGH

Claire HAGGETT



Intégration
environnementale



Lenaïg HEMERY



I. France Energies Marines institute

II. Industrial context

III. Behavior law for mooring design

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V. Multi-scale modeling

Need to find innovative mooring systems for floating offshore wind turbines



Oil platform P-51 off the Brazilian coast is a semi-submersible platform.
Divulgação Petrobras / ABr - Agência Brasil [1]



The Floatgen floating wind turbine, equipped with the Ideal float, installed on the SEM-REV (Centrale Nantes) off Le Croisic.
Credits: Ideol / V. Joncheray

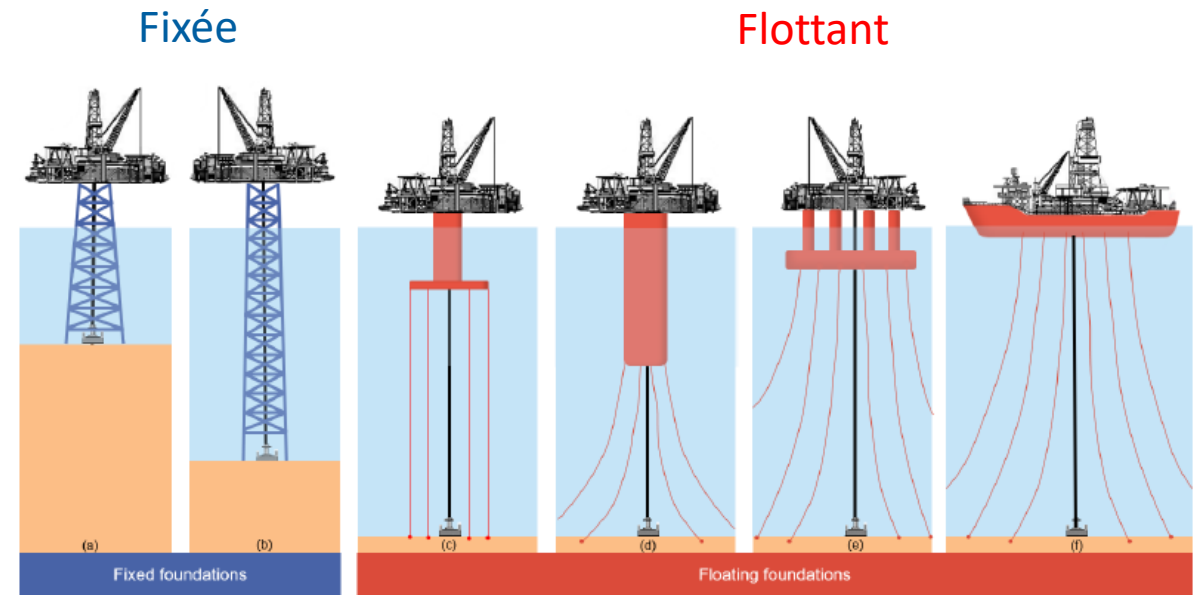
Need to find innovative mooring systems for floating offshore wind turbines

Systemes d'ancrage:

Fonction principale: maintien du flotteur à une position donnée avec une certaine tolérance et avec une certaine souplesse

Fonction secondaire: contribuer à l'amortissement des mouvements

Type d'ancrage: défini par le nombre de lignes, la disposition des lignes d'ancrage et par la composition de celles-ci.



Giovani Aiosa do Amaral. Analytical assessment of the mooring system stiffness. March 2020.

Need to find innovative mooring systems for floating offshore wind turbines

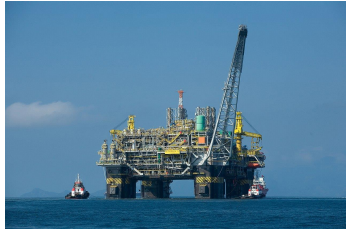
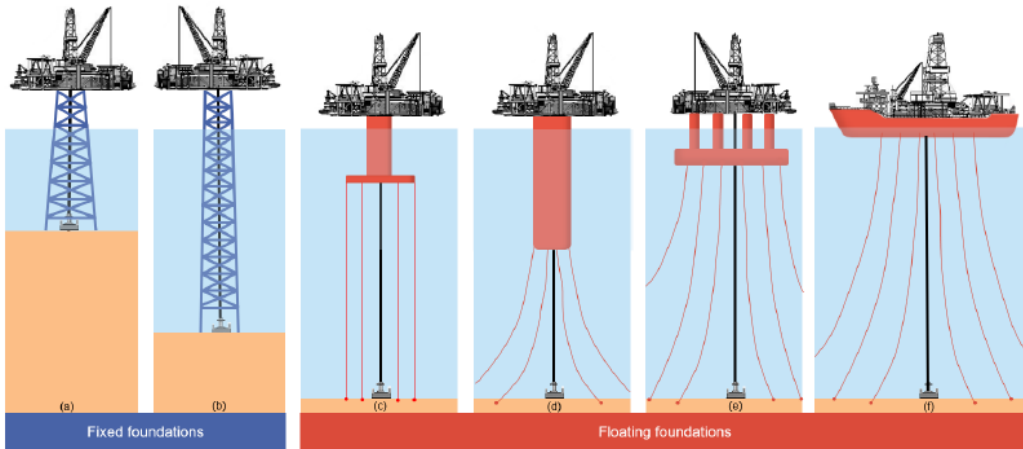


Figure 5 – Offshore Oil & Gas Platforms: (a) fixed, (b) compliant, (c) Tension-leg, (d) Spar, (e) Semi-submersible and (f) Floating Production Storage and Offloading (FPSO).



0 à 60m

Au-delà de 60 mètres

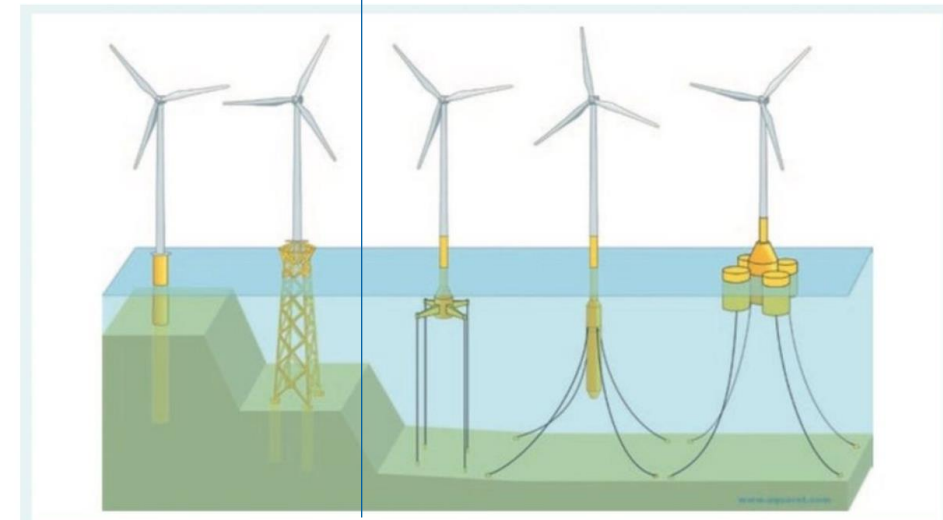


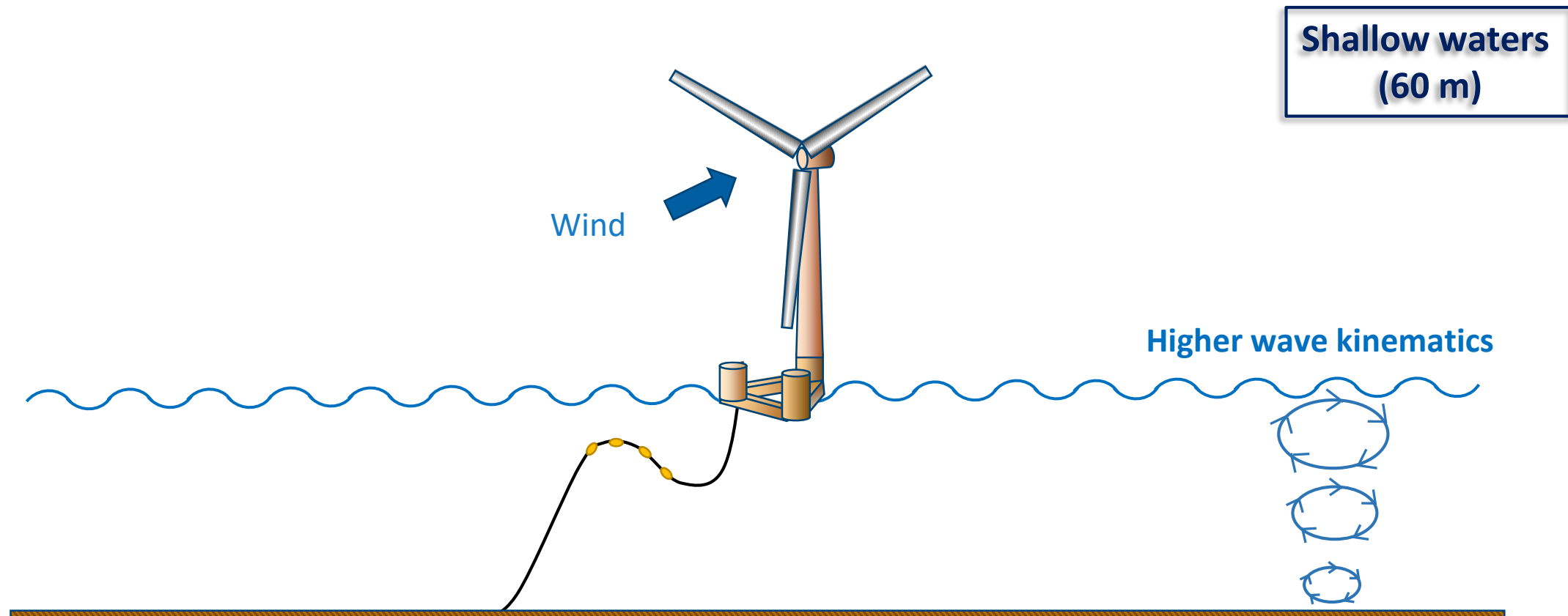
Figure 1: Common fixed and floating offshore wind structure designs (Source: www.aquaret.com). From left to right: driven monopile; steel jacket tower; tension leg platform; spar buoy; semi-submersible

STRATHCLYDE UNIVERSITY

Giovani Aiosa do Amaral. Analytical assessment of the mooring system stiffness. March 2020.

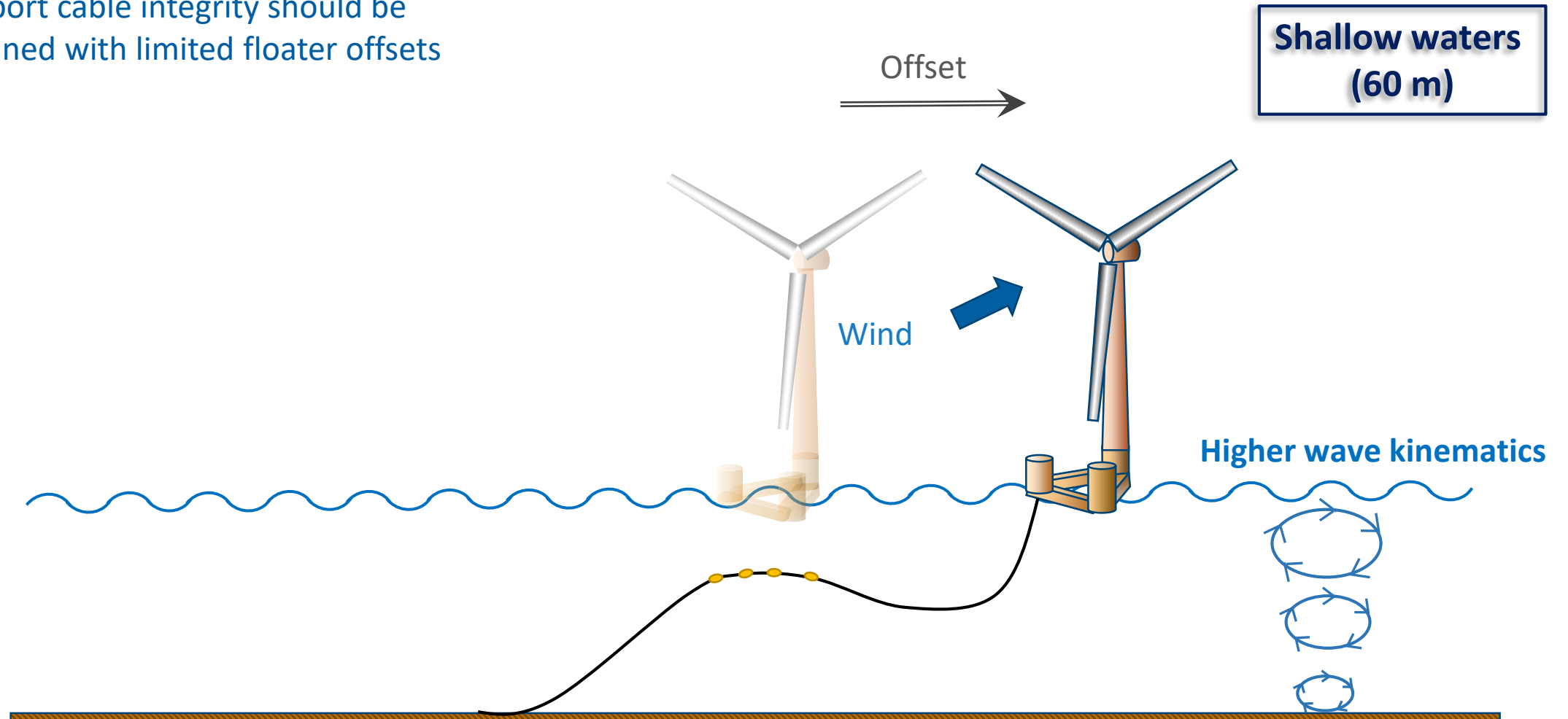
Hannon, M et al (2019) Offshore wind, ready to float? Global and UK trends in the floating offshore wind market. University of Strathclyde, Glasgow, <https://doi.org/10.17868/69501>

Mooring of a floating platform



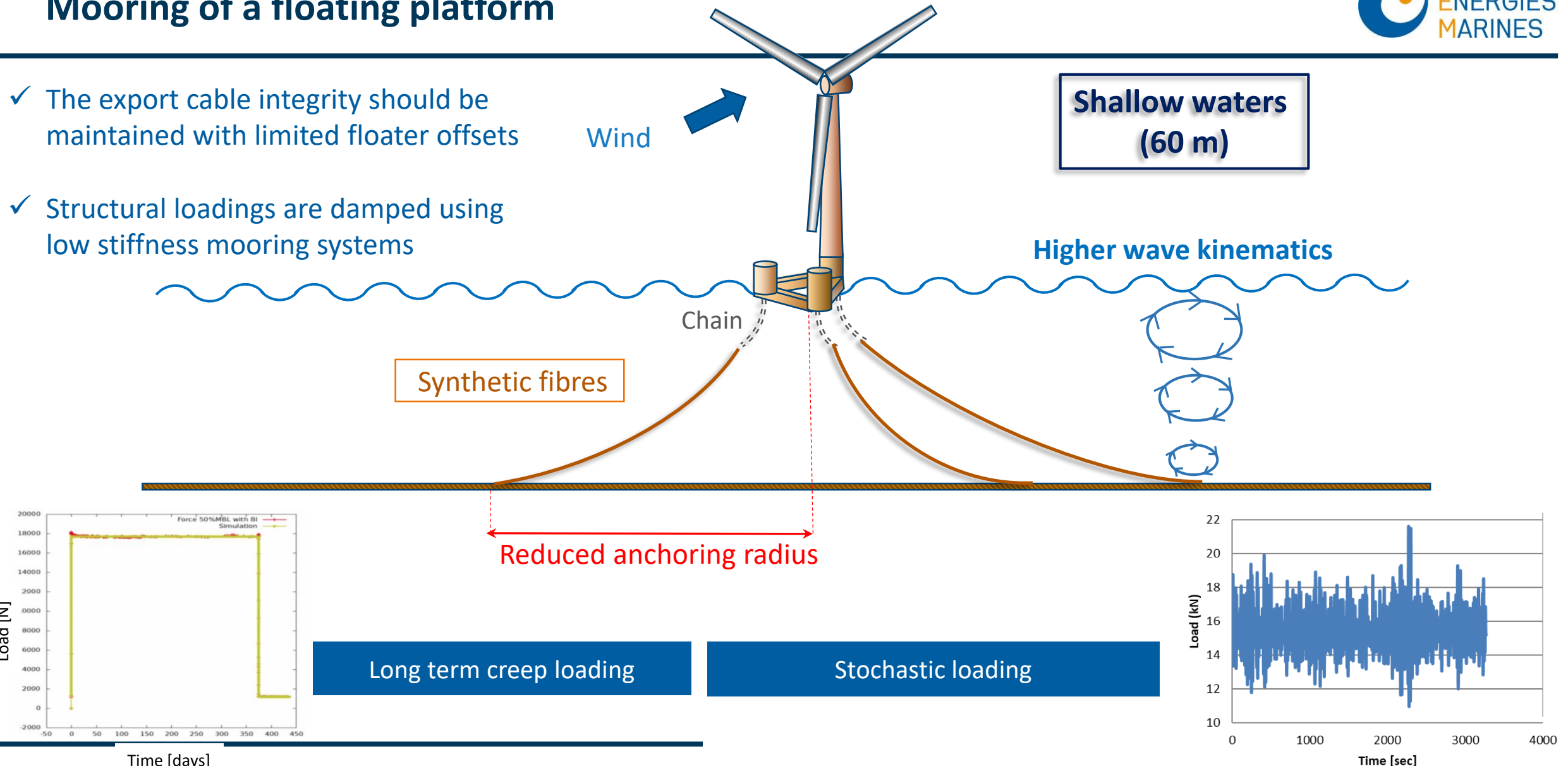
Mooring of a floating platform

- The export cable integrity should be maintained with limited floater offsets



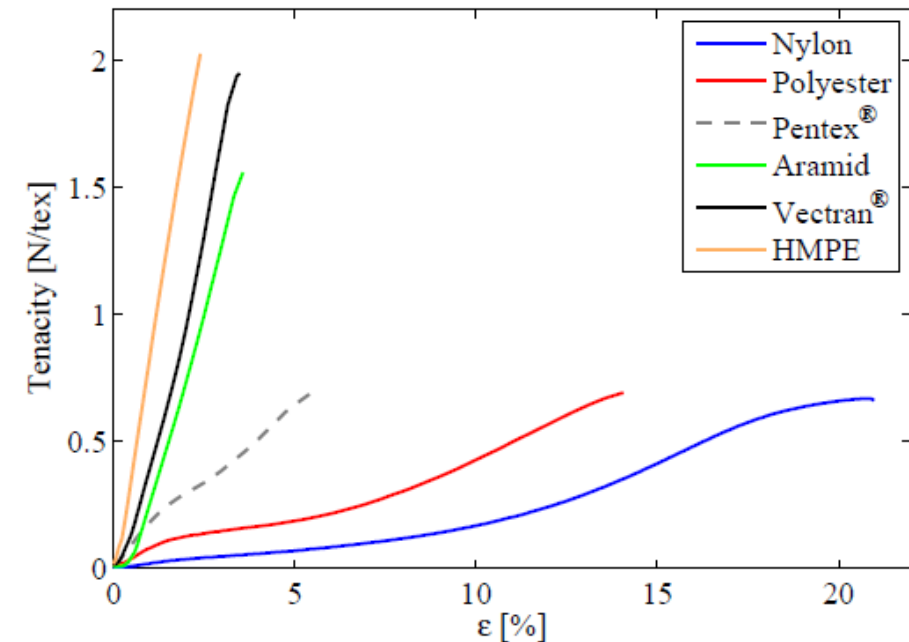
Mooring of a floating platform

- ✓ The export cable integrity should be maintained with limited floater offsets
- ✓ Structural loadings are damped using low stiffness mooring systems



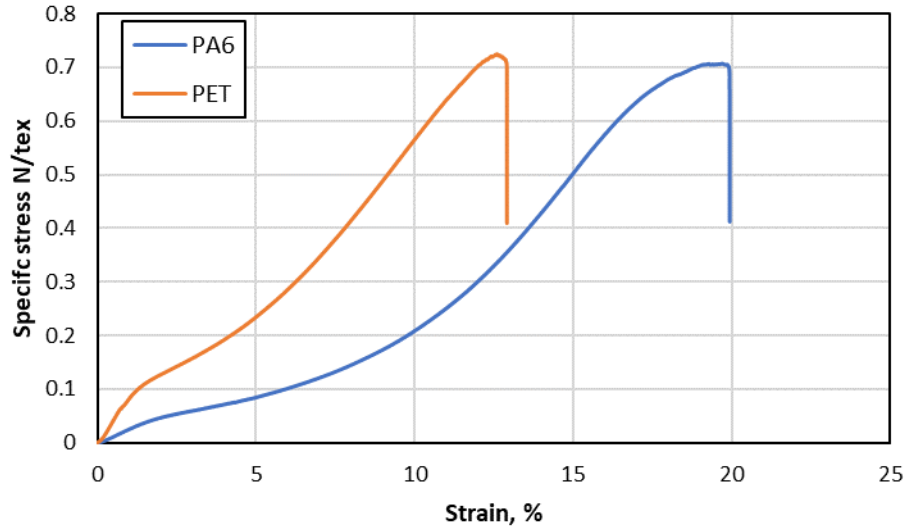
- Polyester, aramid, HMPE, nylon
- Non linear axial stiffness characteristic
- Reduction weight
- High resistance
- Possible reduction in installation cost
- Lack of long term service experience
- Used in permanent or temporary deep-water moorings and for mooring of wind turbines

Typical stress-strain behavior of available synthetic fibres:



Weller, S., Davies, P., Vickers, A., Johanning, L., 2014. Synthetic rope responses in the context of 593 load history: Operational performance. *Ocean Engineering* 83, 111–124. URL: 594

Mooring line: flexible synthetic fibre ropes



Polyester (PET)

Advantages:

- High tension strength
- Fatigue resistance
- Known behaviour

But : Too stiff for shallow waters

Polyamide 6 (Nylon)

Advantages:

- Less stiff
- Good tension strength
- High strain to failure (20%)
- Affordable

But: Only used for short term applications: 2 years.

Weller, S et al. 2015.

		Nylon 6	Polyester
Durability	Ultraviolet light	Good	Good
	Chemicals	Good	Good
	Temperature	Good	Good
	Abrasion	Average	Good
	Creep	Average	Good
	Tension fatigue	Good	Good
	Compression fatigue	Good	Good

Research challenges included in the research projects:

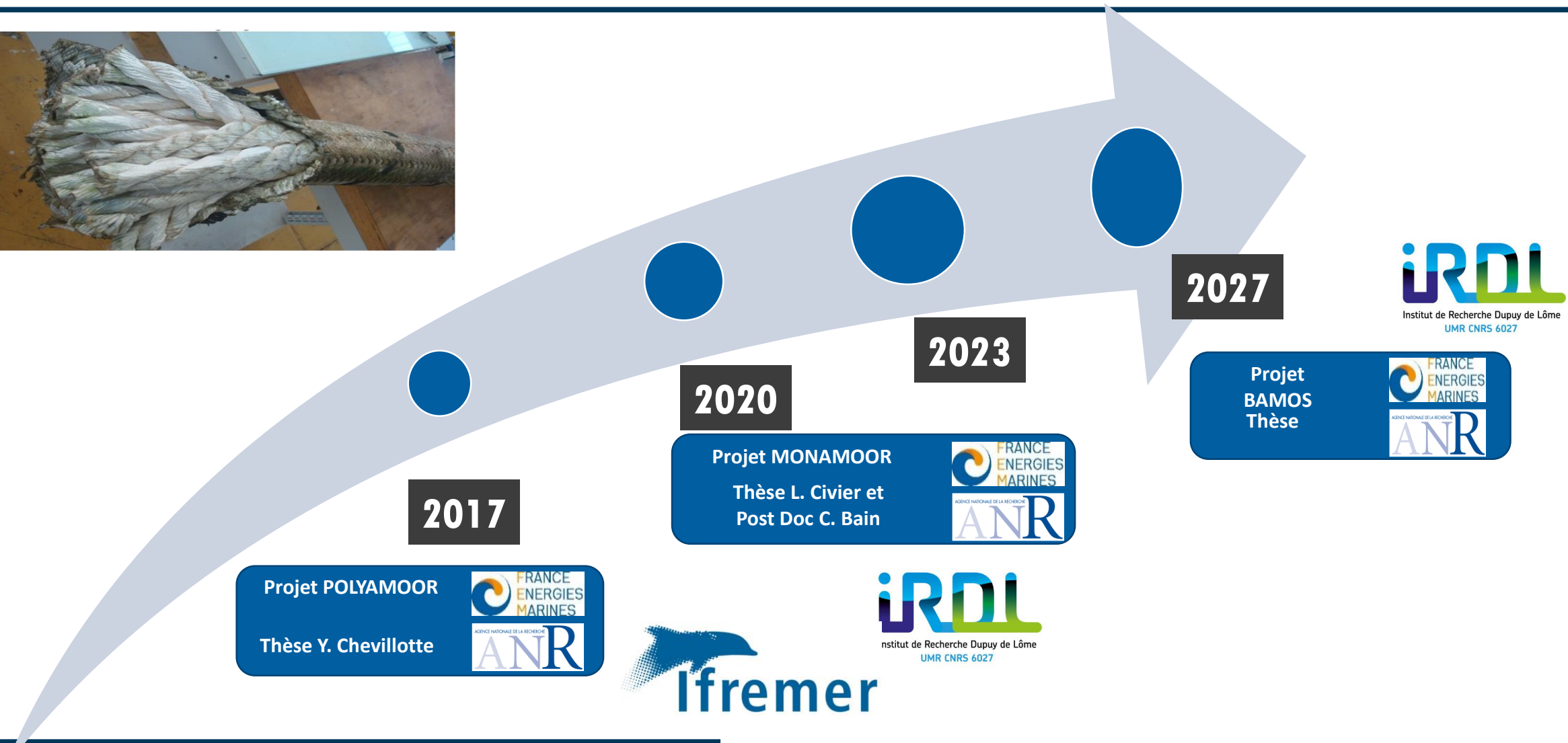
Long term creep behavior

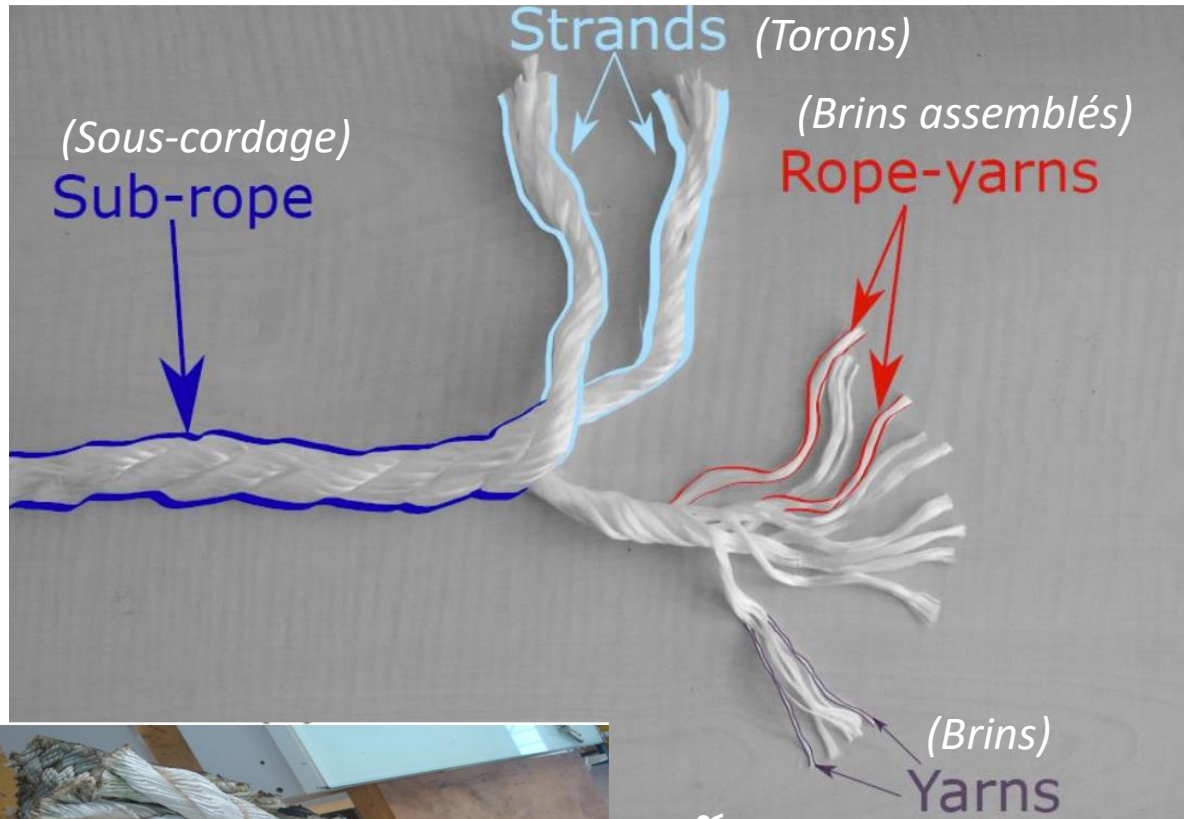
Development of a 3D multi-scale model

Fatigue life and durability

1D constitutive law

Mooring project lead by FEM





BEXCO

Fig: Composition of a polyamide 6 4T sub-rope supplied by BEXCO, Belgium

Important parameters of the construction:

- Lay-angle/Lay-length
- Number of components in each scale
- Diameter
- Coating

Scale:

Laboratory scale: 4T (lay-length: 50 mm)

Full scale: around 30T

Specificities:

- Size of a rope usually defined by its linear density

Textile units : $tex = g/km$

- All ropes have voids
 - Difficult to measure a section
 - Nominal specific stress (N/tex)
 - $1 N/tex \approx 1 GPa$ (average rope)
- Usually mechanical value given in % of Minimal Breaking Load (MBL)

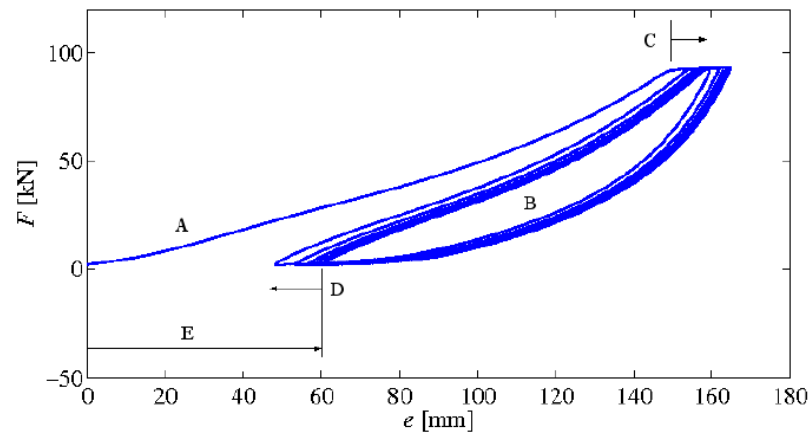
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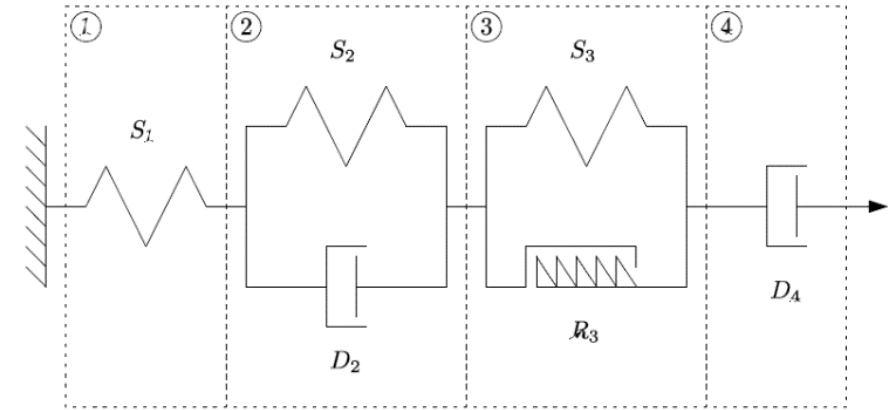
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- The non-linearity and complex behavior of polyamide 6 (visco-elasto-plastic behavior)
- The need to describe and predict this complex behavior for mooring lines application



- Flory's model that helped developed the POLYAMOR law
- François and Davies model (2008) with mean elongation, quasi-static stiffness
- Dynamic response

Context and state of the art

- Model of the elongation-tension relation of mooring line:
 - Usually developed at the scale of the sub-rope
 - Classic method: static stiffness and dynamic stiffness (dedicated tensile tests of BV, DNV ...)
- Issue: some mechanical phenomena are ignored:
 - Permanent elongation (dependent on max. tension)
 - Viscosity (long-term creep, stochastic loading)
 - Loading history dependence (impact of a storm)
- Possible solution = visco-elasto-plastic behavior law of the sub-rope in tension:
 - Syrope spring-dashpot law (polyester sub-rope, no direct identification method)
 - 1D POLYAMOOR visco-elasto-plastic law (polyamide sub-rope, efficient identification method)

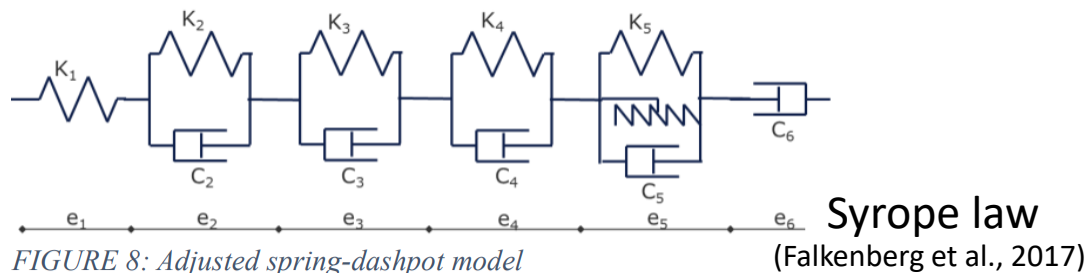


FIGURE 8: Adjusted spring-dashpot model

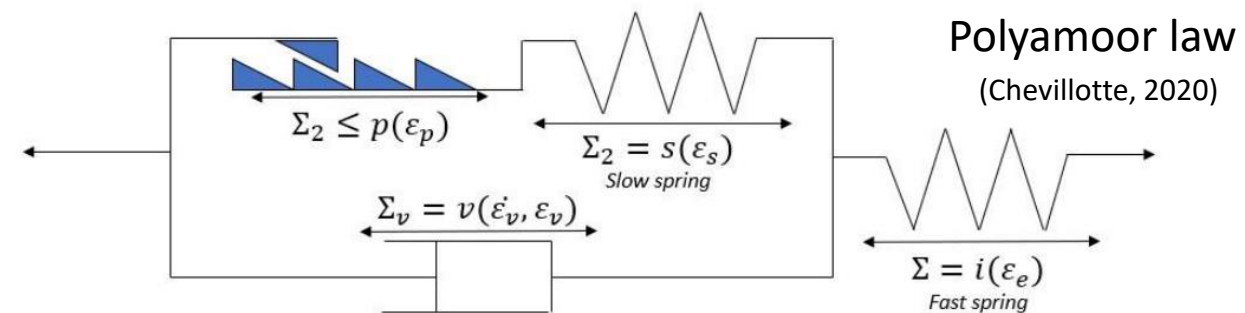
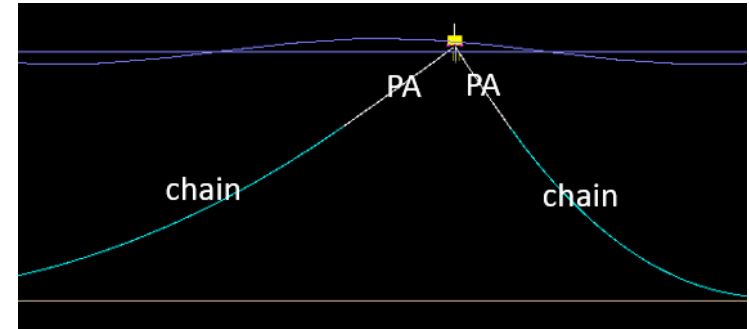
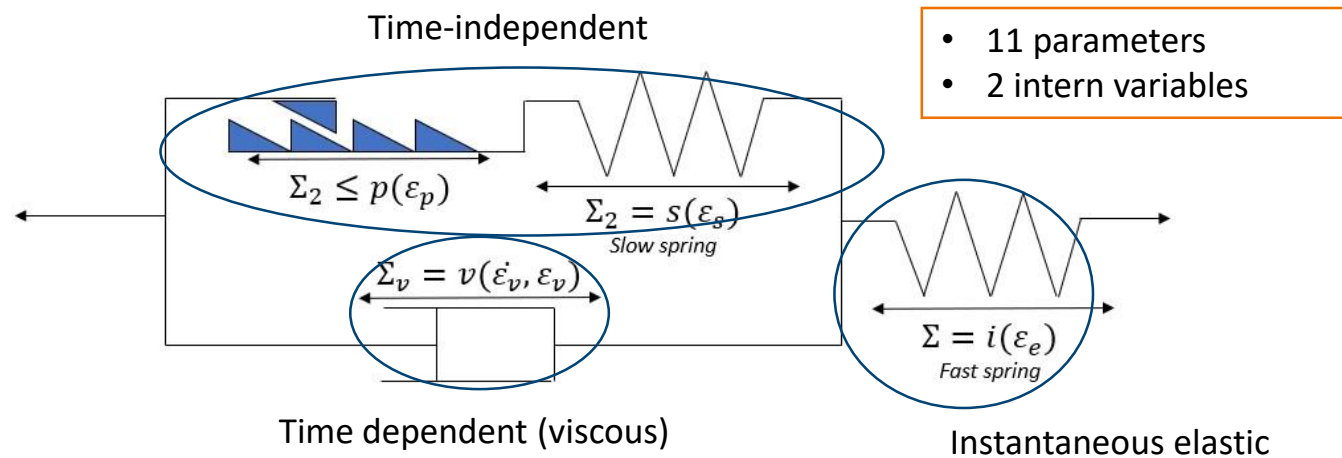


Figure 3.2 - The POLYAMOOR constitutive law

→ Constitutive law developed on 4T scale polyamide sub-rope for floating offshore wind turbines moorings

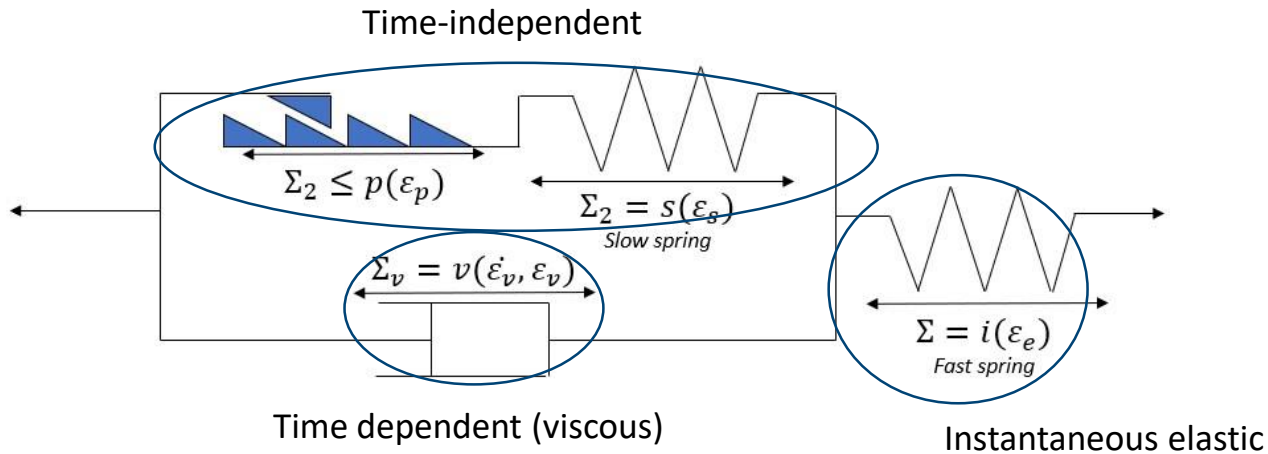


Logiciel DeepLines basé la méthode d'éléments finis dans lequel une première version de la loi POLYAMOOR est implémentée

With the POLYAMOOR law, we aim at:

- Describing the behavior of nylon 6 and taking into account: the history of loading, fatigue and cyclic response, creep, relaxations.

POLYAMOOR law description



- 11 parameters
- 2 intern variables

$$i(\epsilon) = \frac{b}{a} \cdot (e^{a \cdot \epsilon} - 1)$$

a [-]
 b [N/tex]

$$d(\epsilon) = \frac{g}{c} \cdot (e^{c \cdot \epsilon} - 1)$$

c [-]
 g [N/tex]

$$p(\epsilon_p) = e \cdot (\tanh(f \cdot \epsilon_p + h) + 1) \text{ if } \epsilon_p \leq \frac{-h}{f}$$

$$p(\epsilon_p) = e \cdot (f \cdot \epsilon_p + h + 1) \text{ if } \epsilon_p > \frac{-h}{f}$$

e [N/tex]
 f [-]
 h [-]

$$\Sigma_v = v(\dot{\epsilon}_v, \epsilon_v) = W_2(\epsilon_v) \cdot \sinh^{-1} \left(\frac{\dot{\epsilon}_v}{W_1} \right)$$

W_1 (s⁻¹)

$$W_2(\epsilon_v) = a_{w2} \cdot \epsilon_v^\alpha + b_{w2}$$

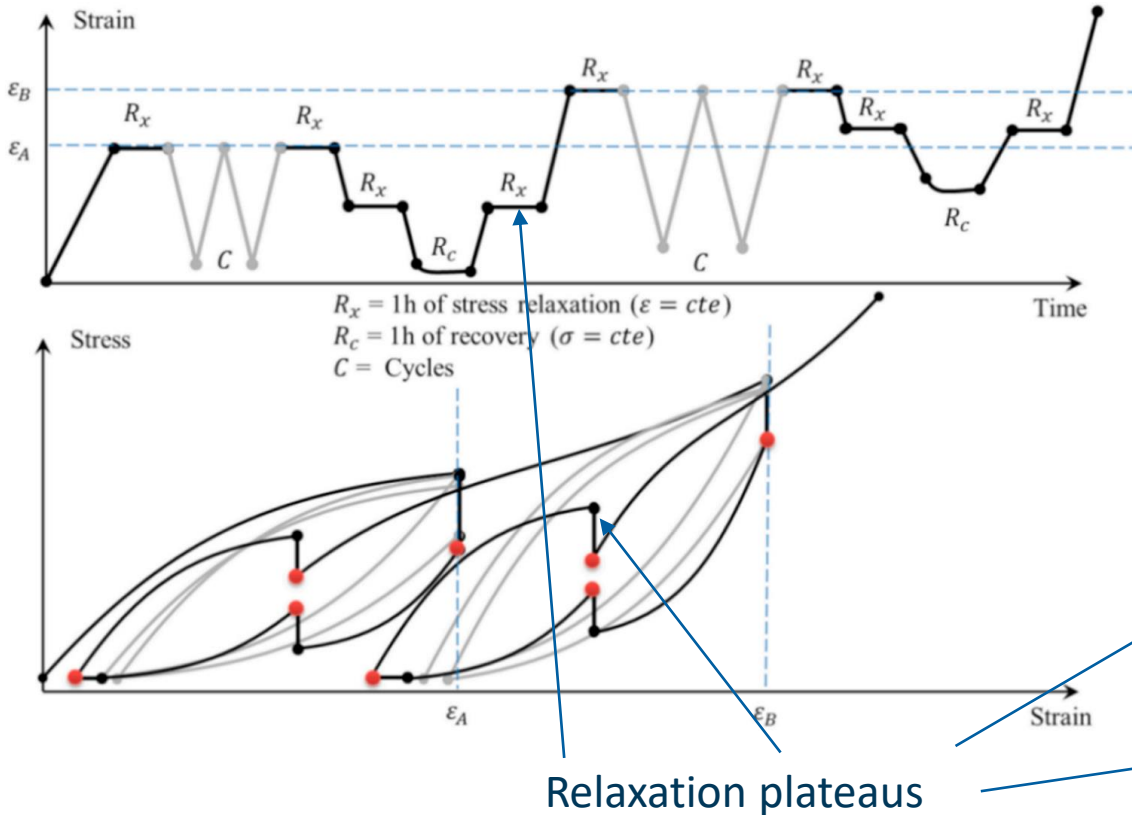
α [-]
 a_{w2} [N/
 b_{w2} [N/

The one-dimensional spring-dashpot-ratchet law is represented in and has the following elements:

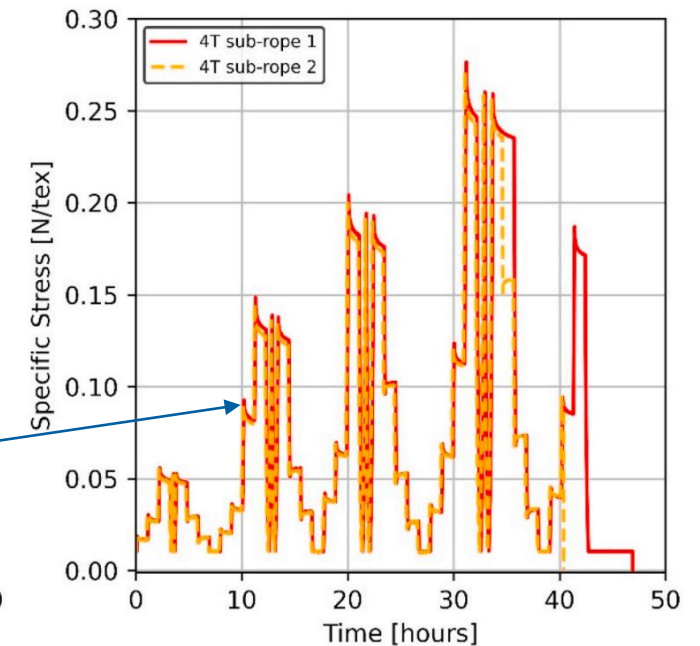
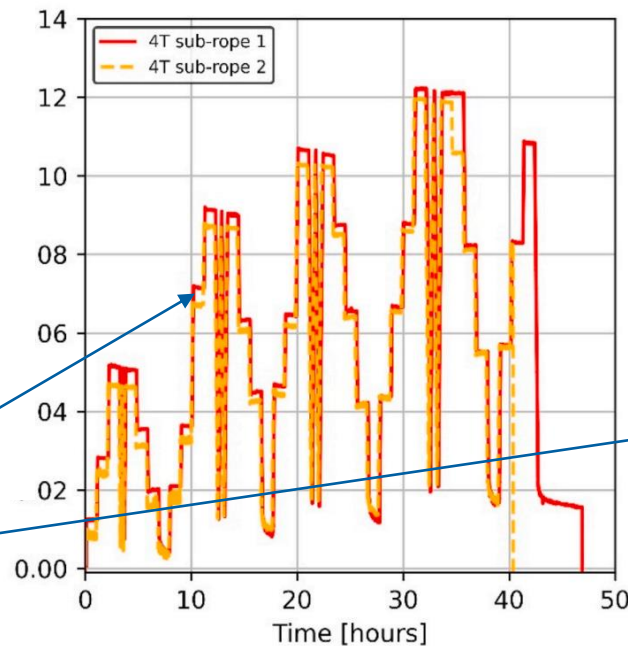
- **A fast spring** describing the dynamic behavior,
- **A dashpot** responsible for the viscous stress of the polymer,
- A time-independent part consisting of a **ratchet element** for the plasticity, and a **slow spring** responsible for the relaxed elasticity.

POLYAMOOR law: identification method

- Parameters identification from a multi-relaxation test



L.Civier, Y.Chevillotte, C.Bain, G.Bles, P.Davies, Y.Marco, Visco-elasto-plastic characterization and modeling of a wet polyamide laid-strand sub-rope for floating offshore wind turbine moorings, Ocean Engineering (2024)



POLYAMOOR: Test set ups needed

Law identified used a multi-relaxations test procedure:

- Strain interval: 0 to 12%
- Strain rate: 10^{-5} s^{-1}



Figure: Servotest machine used in the laboratory of ENSTA Bretagne [1]

Small scales



Figure: Ifremer test bench

Middle and high scales

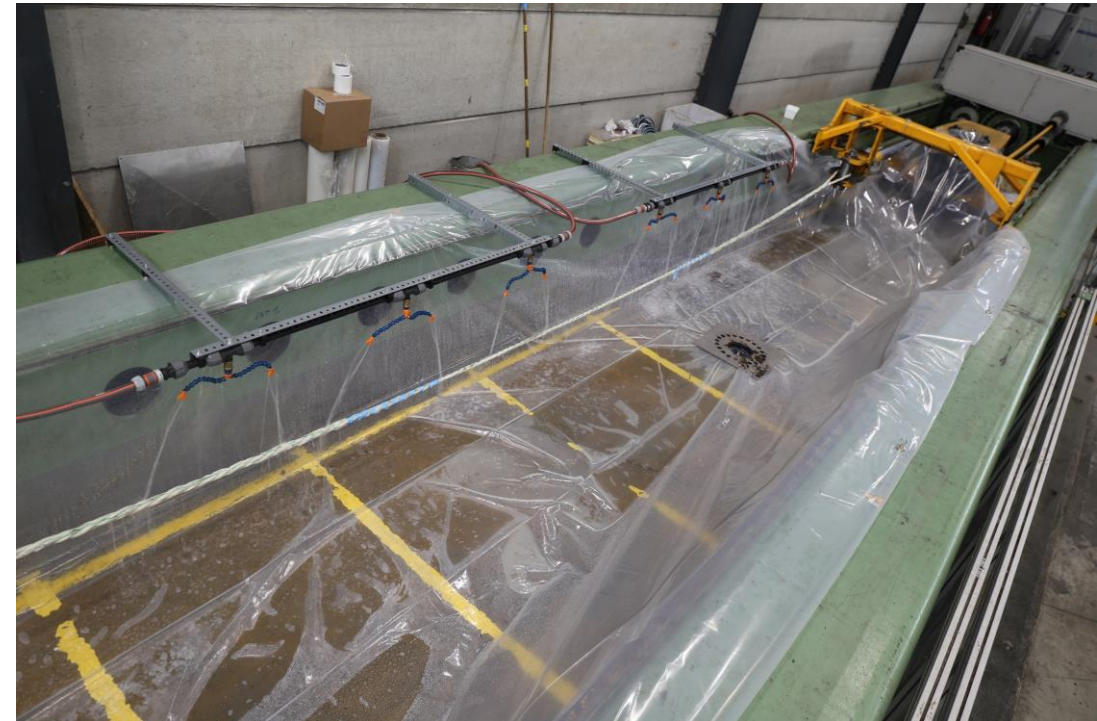


Figure: BEXCO test bench

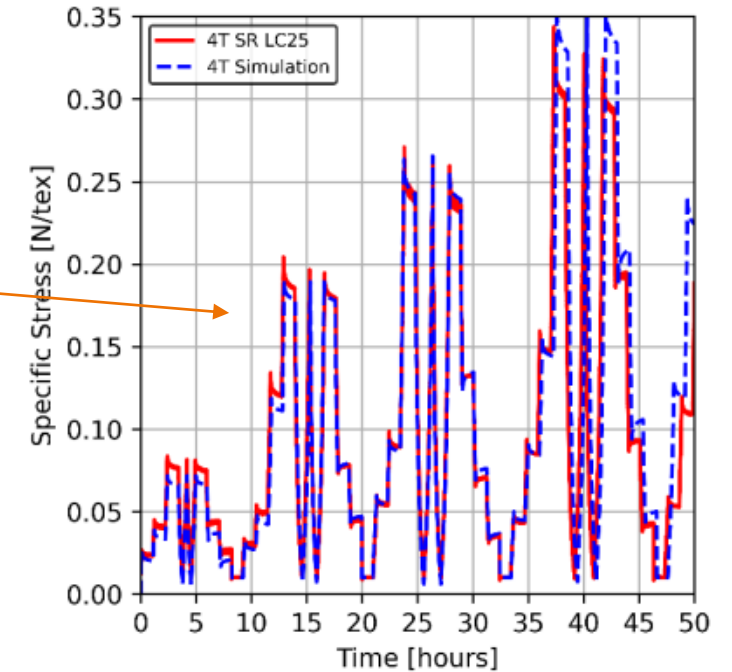
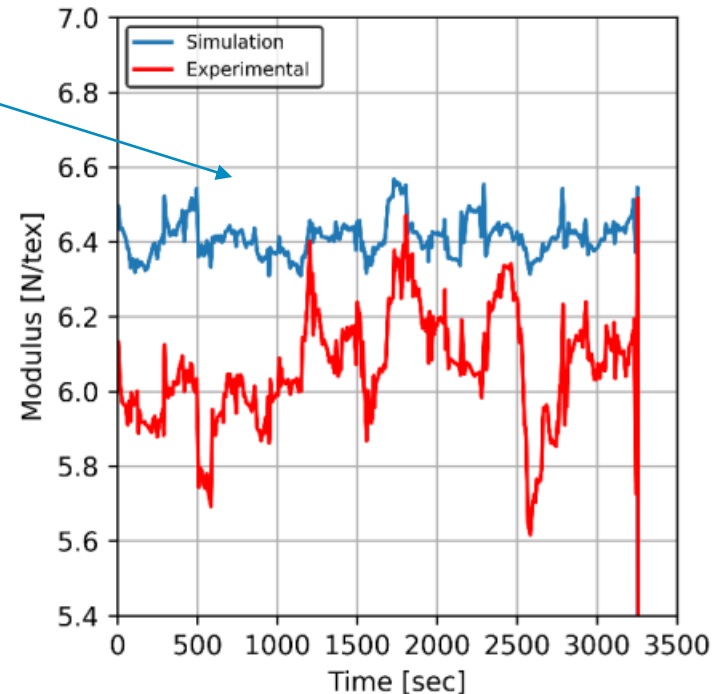
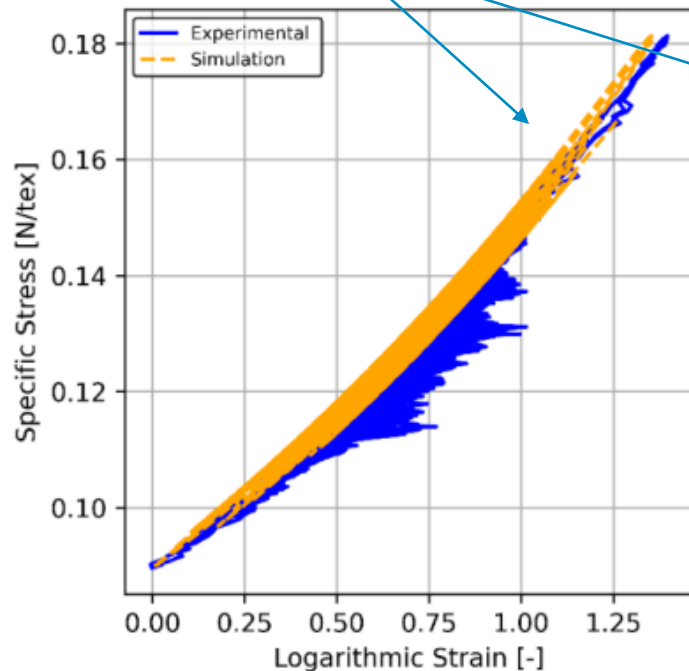
High scales

First validation of the law on small scales/middle scales

• Law POLYAMOOR is accurate for tests of:

- Short creep
- Multi-relaxation
- Multi-creep
- Stochastic loading

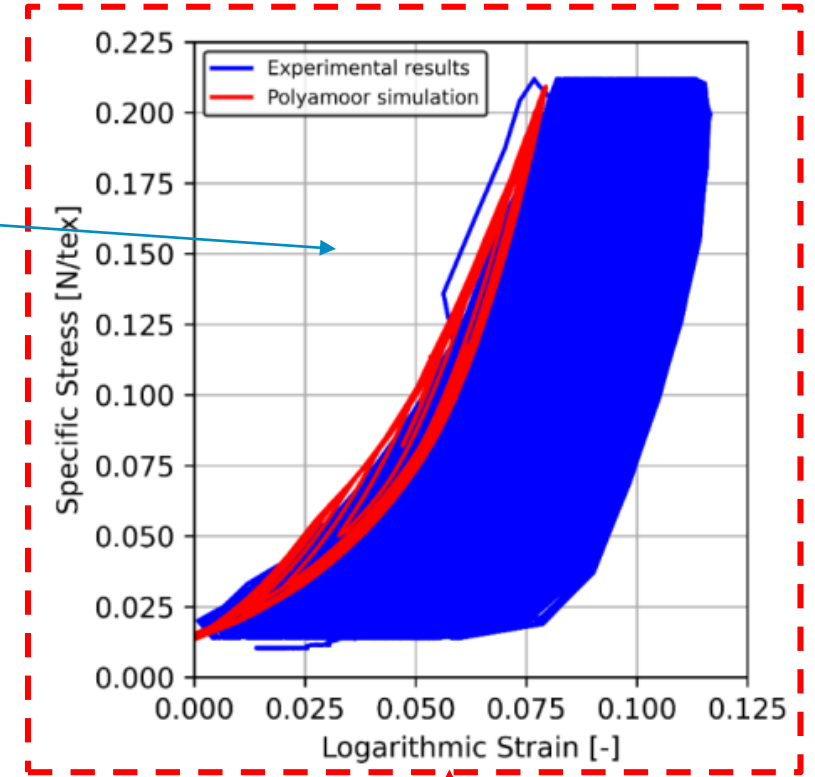
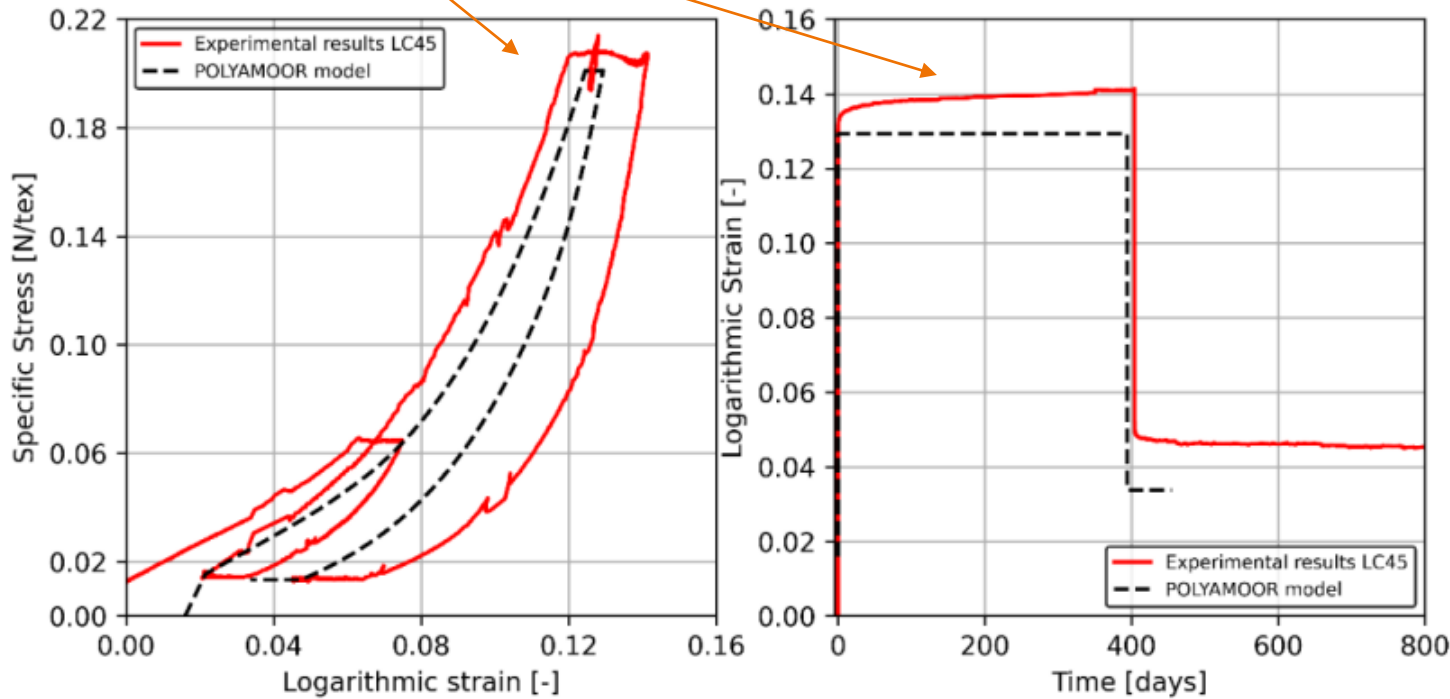
Characteristic times:
few secondes to few hours



First validation of the law on small scales/middle scales

- Law POLYAMOOR is not accurate for tests of:
 - Long-term creep
 - Fatigue, above a certain number of cycles

Characteristic times:
few hours to months



Questionable: only one test !

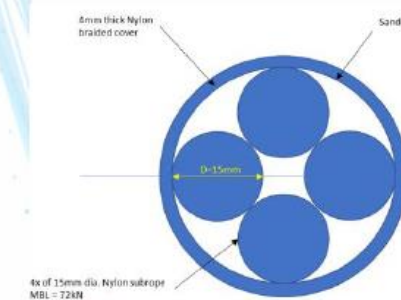
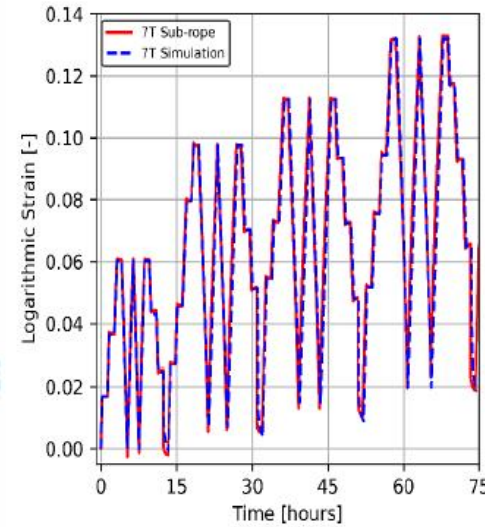
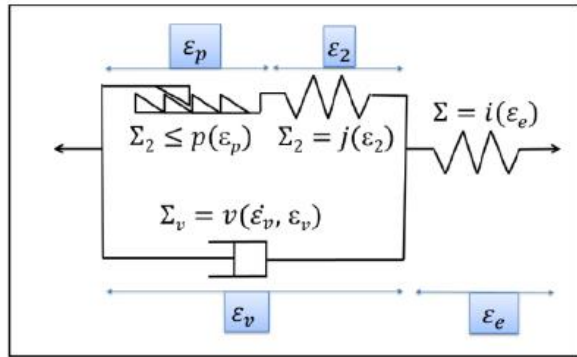
Comparison with at sea trials

POLYAMOOOR
behavior law

Law parameters
identification process

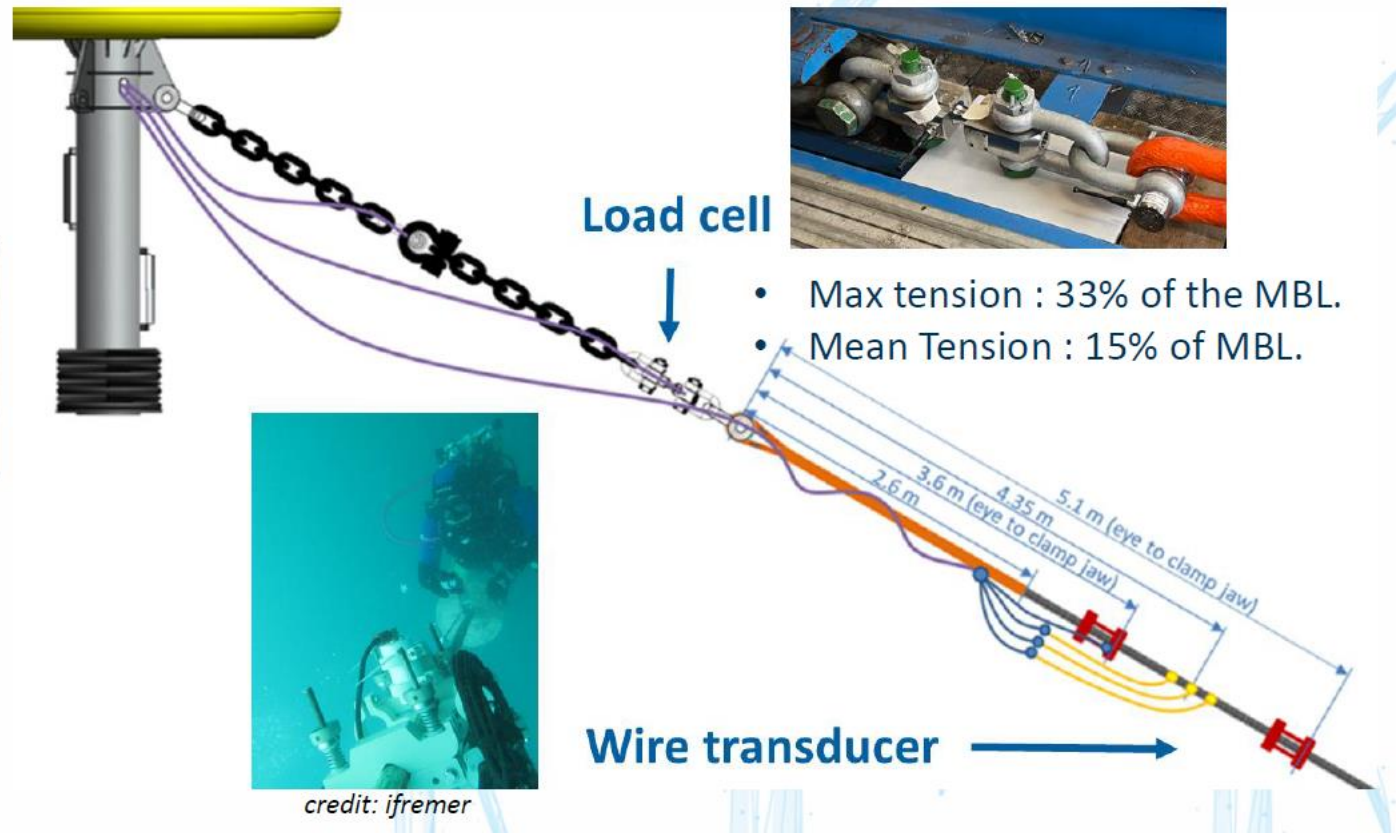
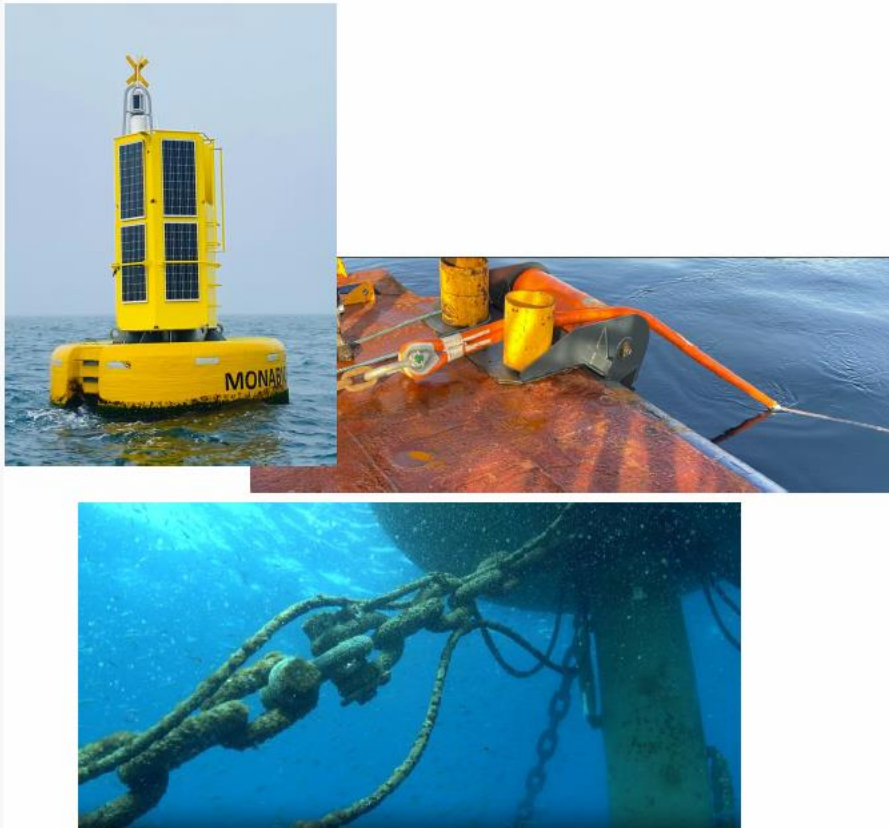
Validation of the law
in lab

Monitoring at sea



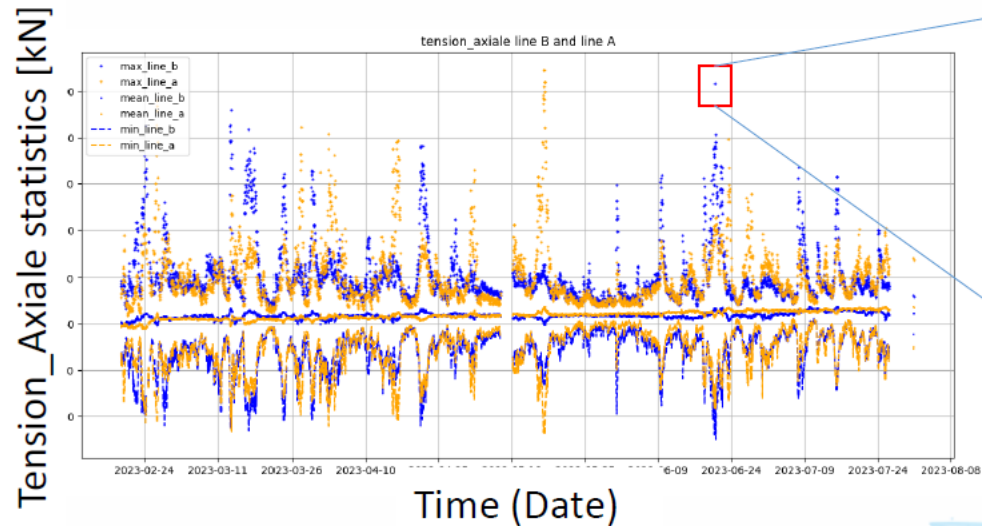
At sea-trials: buoy moored with experimental set up

Experimental set-up :



Measurements obtained

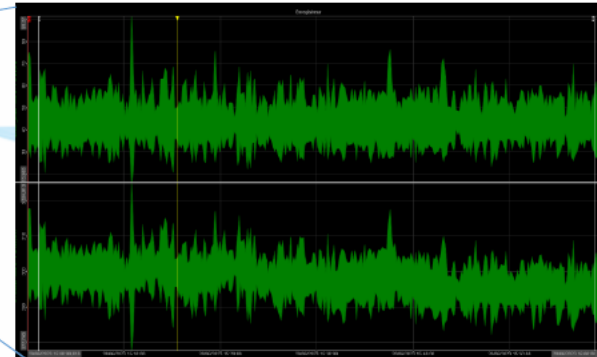
Long term measurement dataset



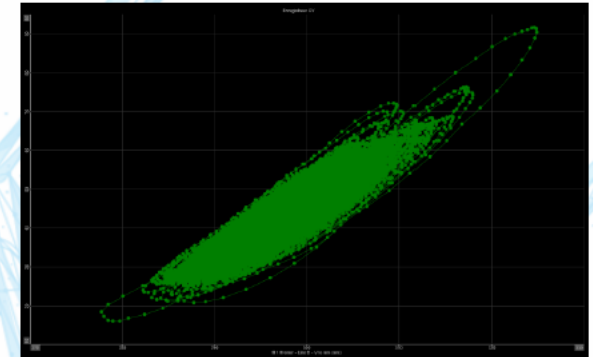
- **Mean tension has been almost stable.**
- Maybe sensor drift, to be checked at sensor recalibration.
- Several high load events before the selected one.

Dataset Available with measurements from Feb. 23 to Aug. 23

Zoom on 20/06/2023



Tensions and elongation time series



Elongation vs. tension

- Sensors are time synchronized
- Sensor data @ 10Hz

Deeplines Model set-up

- Pure traction test set-up.
- Impose of tension sensor recording @ 10Hz

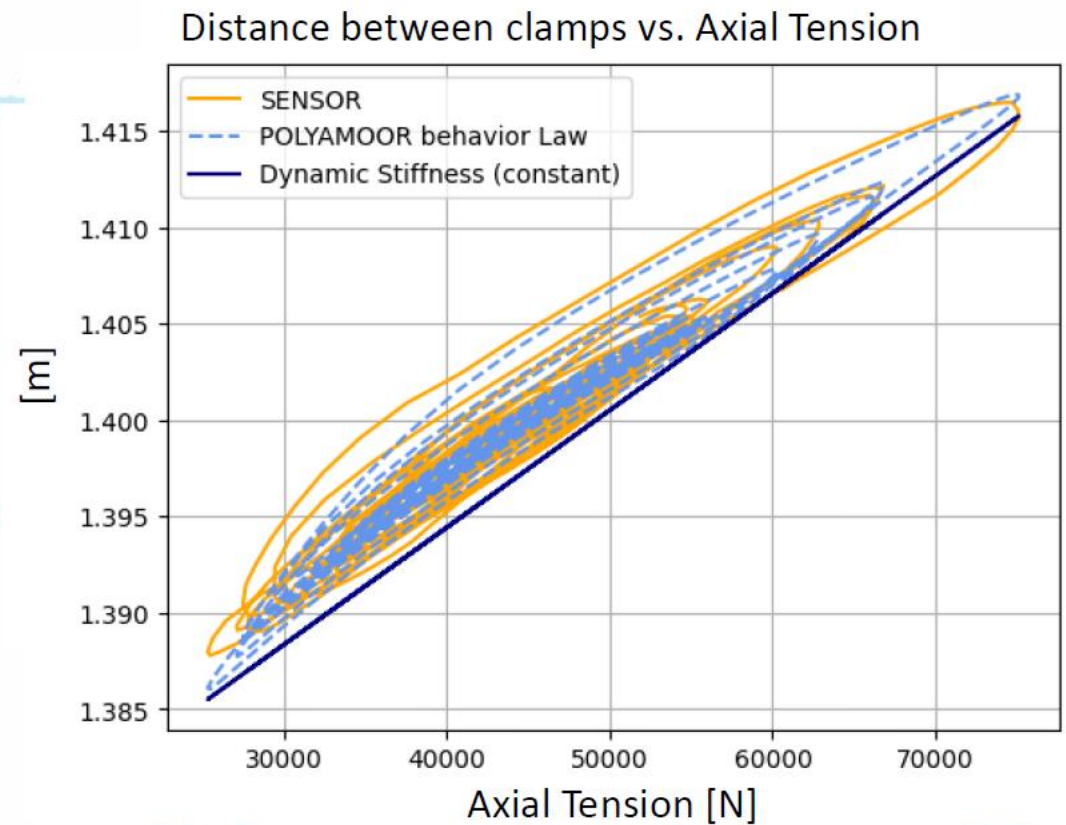
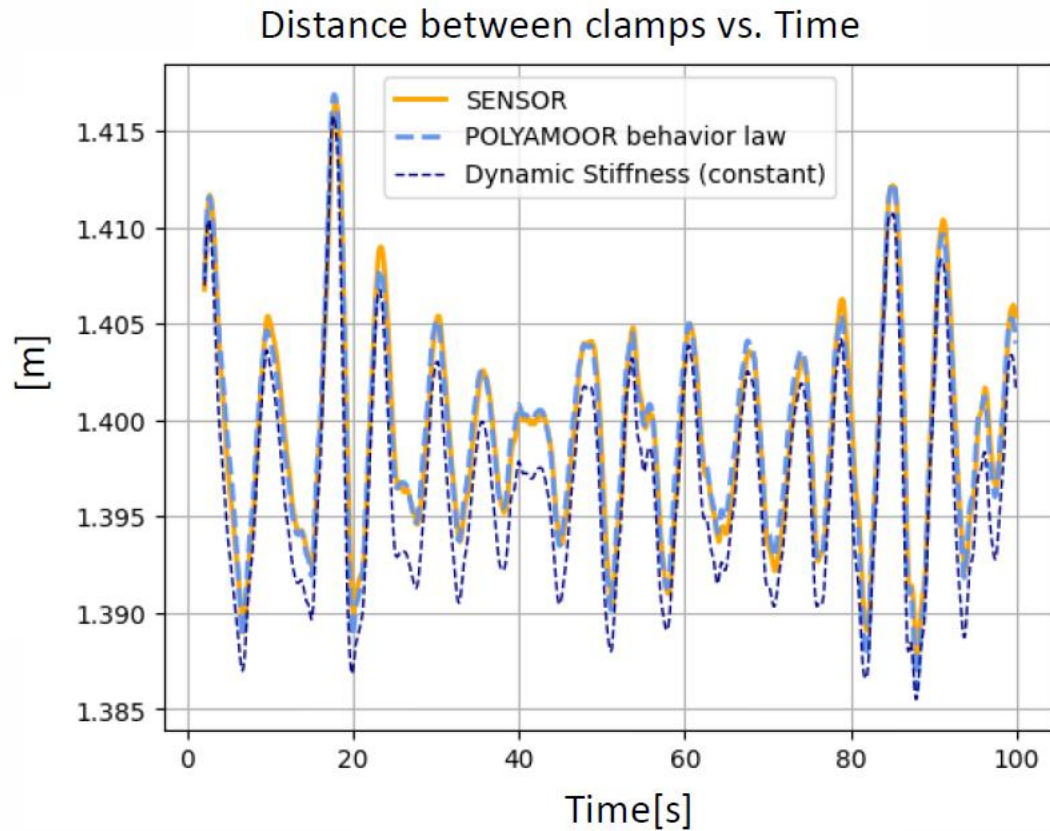


Compare POLYAMOOR behavior law vs. dynamic stiffness law

	POLYAMOOR behavior law	Dynamic stiffness
Constant parameters for all load cases	✓	⊗
Available in most commercial software	⊗	✓ ⊗
Model during dynamic simulation	$T = f(\epsilon, \dot{\epsilon})$	$T = Kd(T_{mean}, T_{amp}) * \epsilon$
Model viscosity & plasticity	✓	⊗

Cross validation of model behavior laws & elongation sensor measures

Cross validation of model behavior laws & elongation sensor measurements



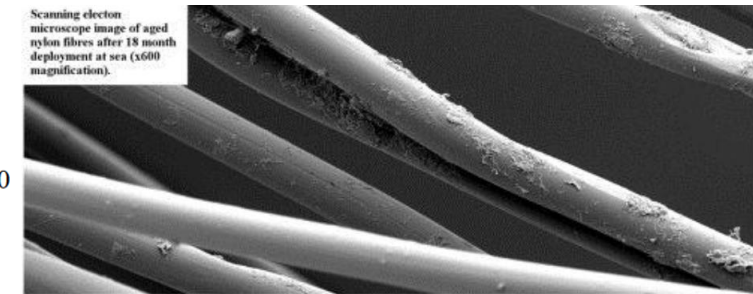
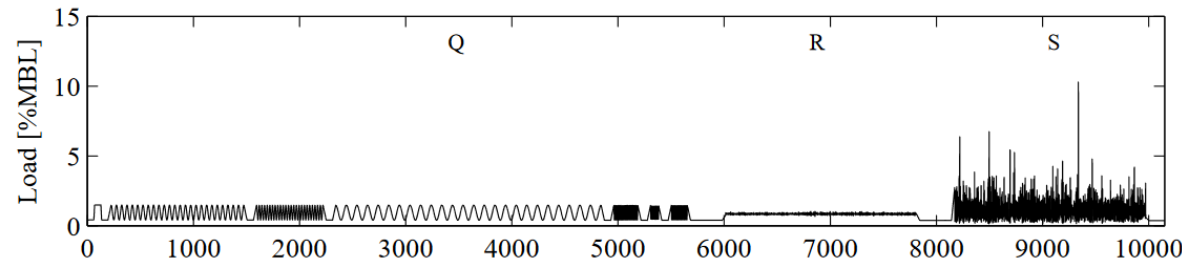
Used ropes campaign: bibliography

Experimental test performed on a laid polyamide rope after 18 month deployment in sea (WEC application).

Rope construction: 7 parallel-stranded sub-rope covered by a non-bearing-load cover and without filter cover

Experimental test campaign performed on the aged rope:

- Quantification of the marine growth: weight and diameter measurements
- Aged sub-rope and yarn assemblies subjected to: harmonic loading, tension fatigue, tensile test to failure
- SEM images
- Yarn-on-yarn abrasion test



Scanning electron microscope image of aged nylon fibres after 18 month deployment at sea (x600 magnification).

Conclusions:

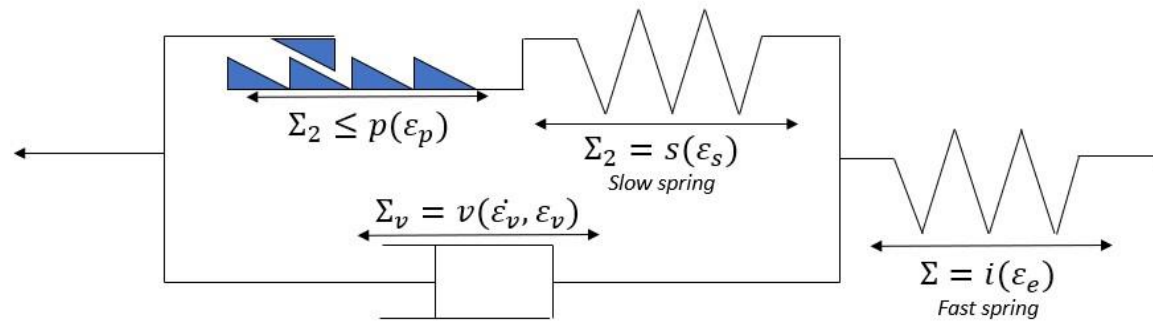
- Aged yarns showed lower performances
- Due to two main damage mechanisms: abrasion wear between outer yarns and jacket due to sediment and mussel infiltration (external abrasion/damage) and fibre-on-fibre wear during tension fatigue

Weller, S.D., P. Davies, A.W. Vickers, et L. Johanning. « Synthetic Rope Responses in the Context of Load History: The Influence of Aging ». *Ocean Engineering* 96 (mars 2015): 192-204.

<https://doi.org/10.1016/j.oceaneng.2014.12.013>

Enhanced 1D behavior law for PA rope and scale effect

- Identification of the viscous parameters on the MONAMOOR long-term creep data.
- Identification of the whole set of parameters on longer-term multi-relaxation tests (2 or 3-hour-long plateaus instead of 1-hour currently)
- Tests and identification of the POLYAMOOR 1D law on higher MBL sub-rope (7T, 25T, 45T)



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II. Industrial context

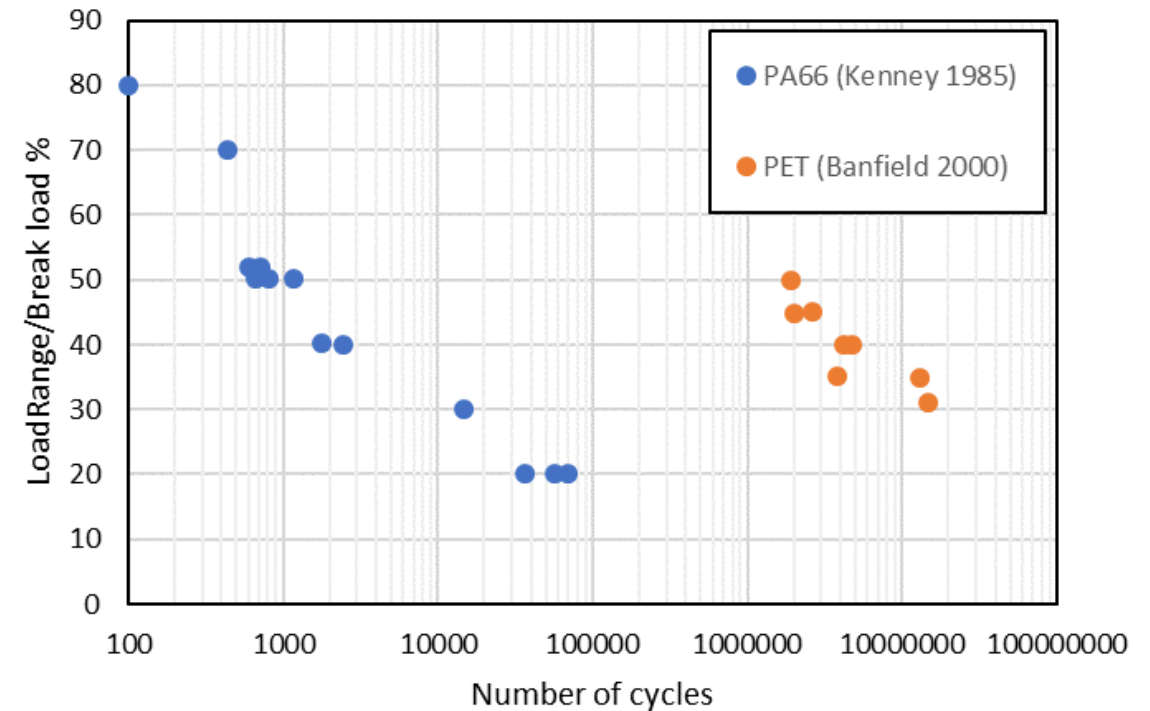
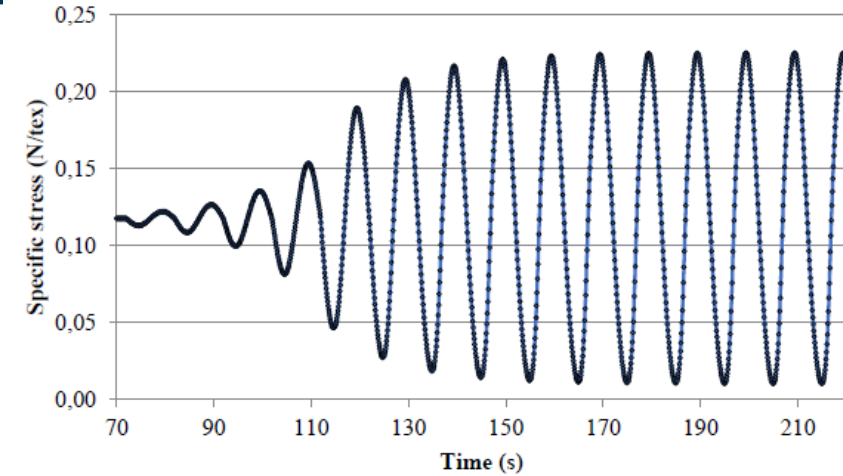
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Fatigue study: state of the art

Fatigue → degradation and failure induced by repeated loading
Key limitation for polyamide ropes



Fatigue study: state of the art

Fatigue → degradation and failure induced by repeated loading
Key limitation for polyamide ropes



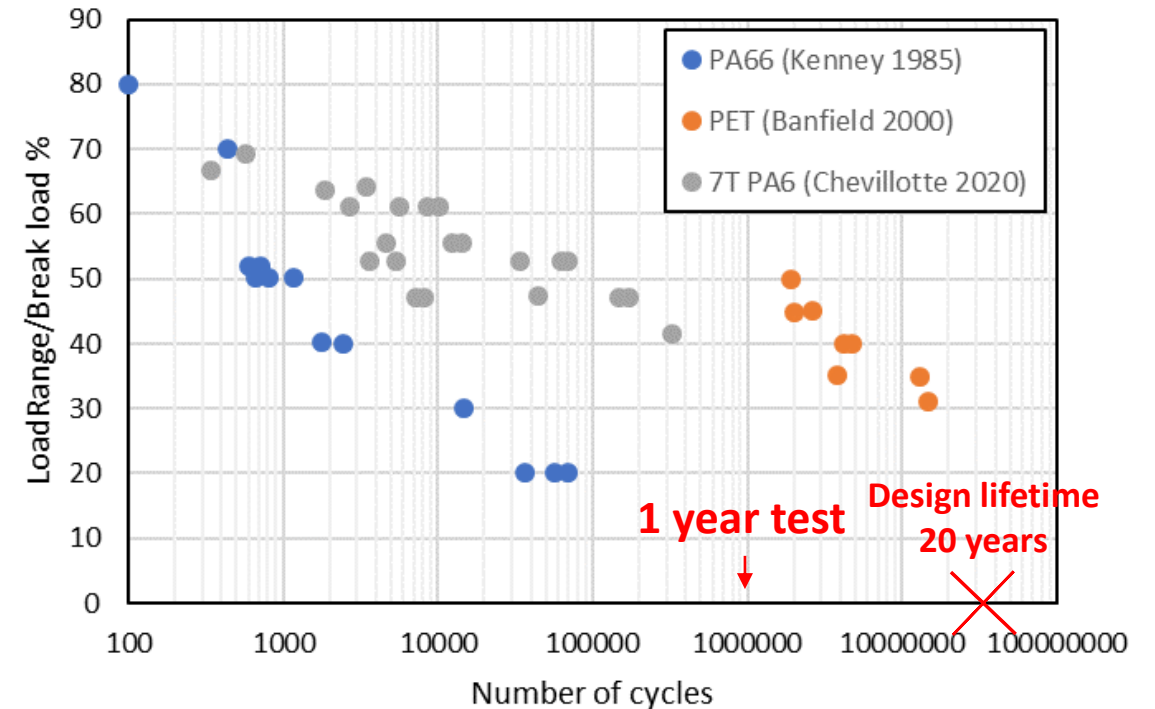
What are the damage and failure mechanisms ?

- At the fibres scale (Herrera *et al.* 2004):
 - Creep
- At the strands and sub-ropes scale: (Parsey *et al.* 1983)
 - **Structural fatigue**
 - **Internal abrasion**

→ Evolution of the construction and coating to increase fatigue durability: **provide a suitable fatigue lifetime.**

→ Better understand the construction impact on fatigue and perform screening of construction

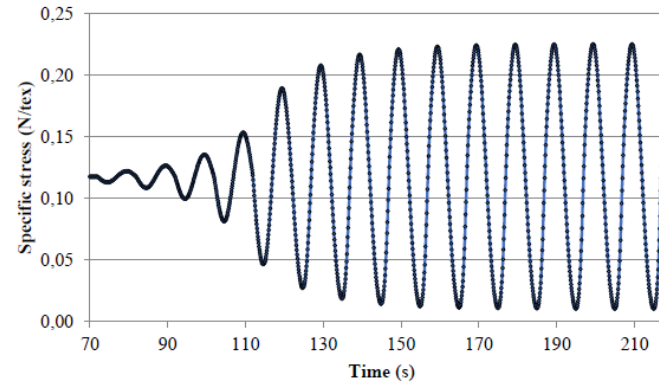
→ Development of a model



Experimental set up

Fatigue campaign:

- Frequency of 0.1 Hz
- Between a fixed minima at 2 %MBL and varying maximal (R ratio close to 0)
- Fatigue test stops at the failure of the specimen



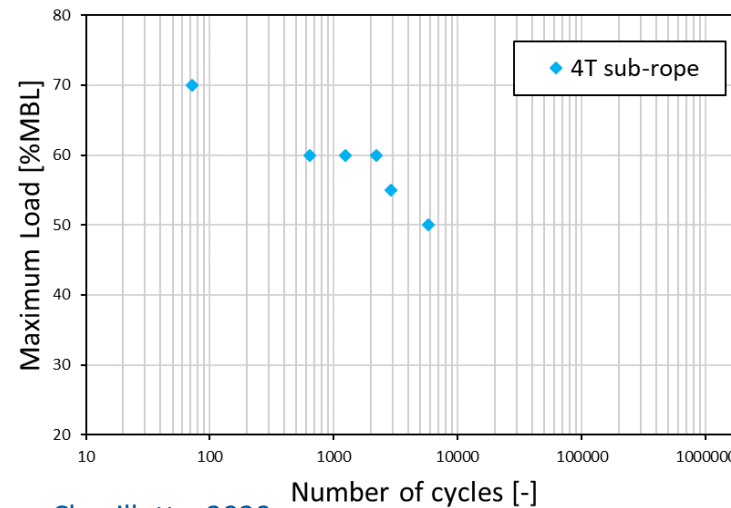
Study of the laboratory scale: 4T

900 mm long sample with two splices manually made

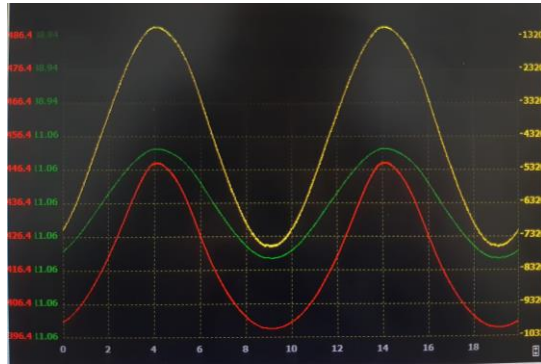
Immersion of the sub-rope at least 24h before the test

Rope maintained wet during the test

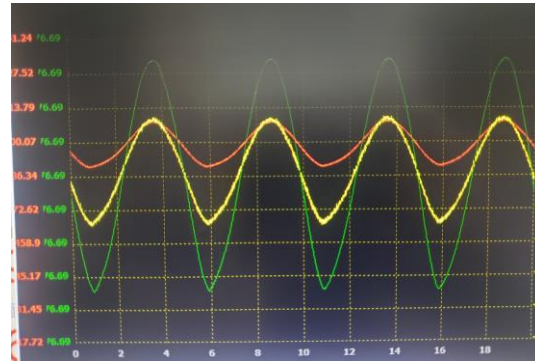
Watering system



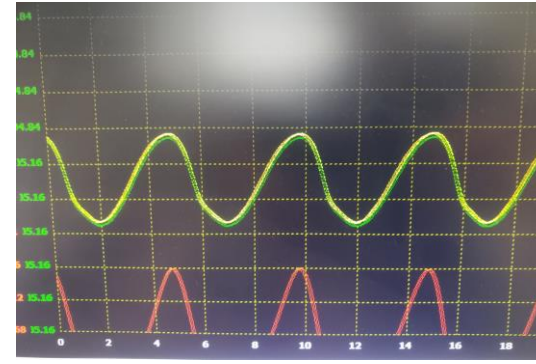
March-may 2024 fatigue campaign



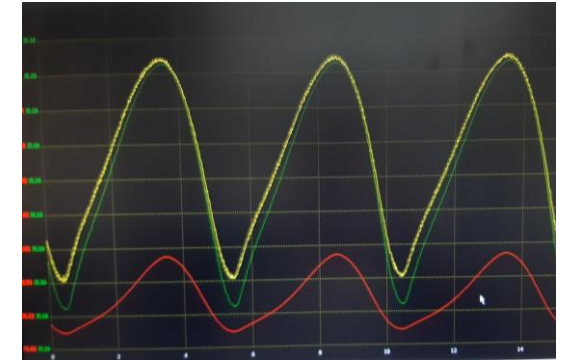
0,1 Hz



0,2 Hz

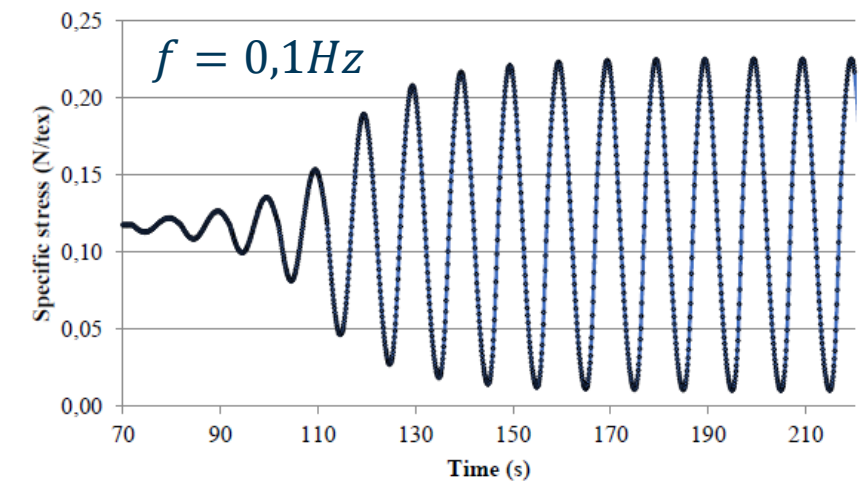


0,2 Hz



0,2 Hz

Not possible to increase frequency, we keep 0,1 Hz.

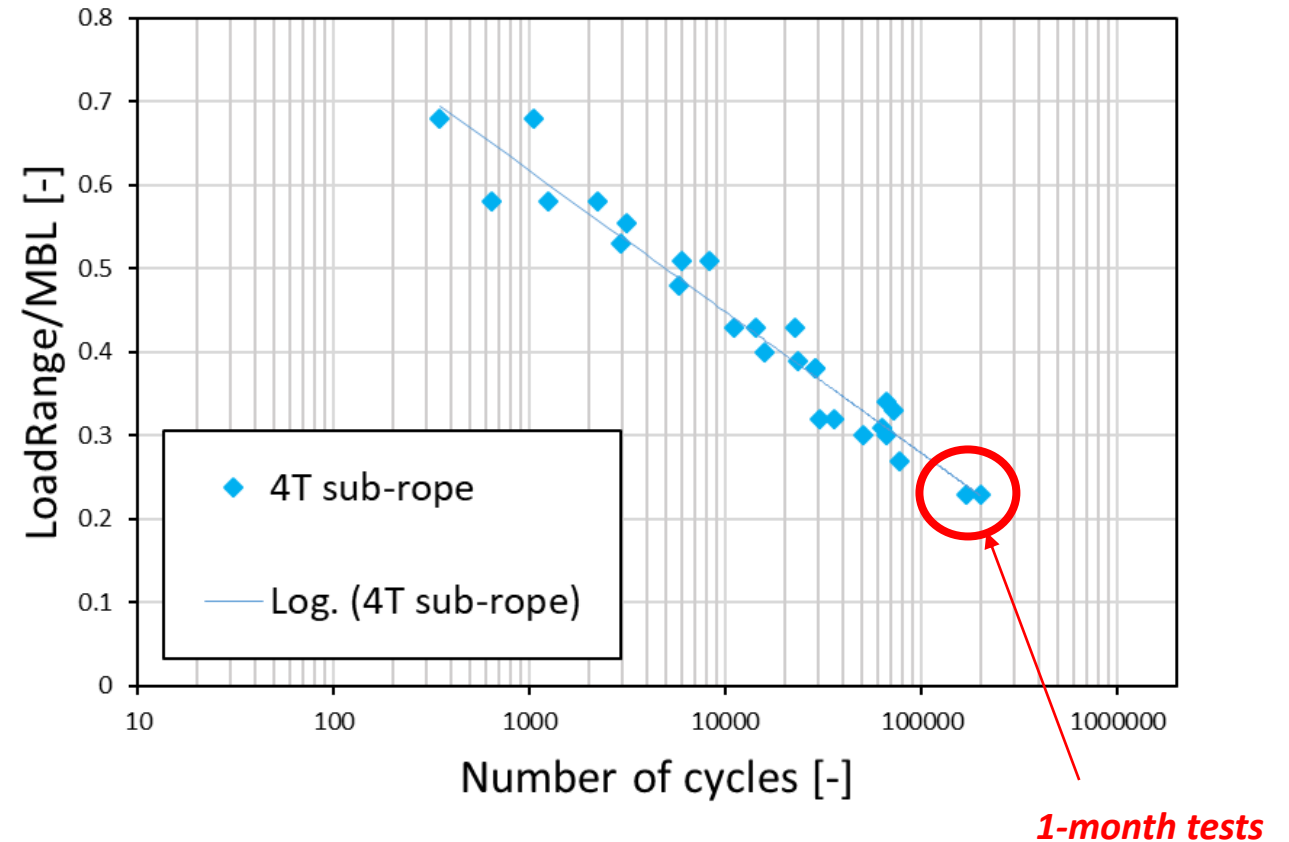


10 cycles to set-up the load amplitude value

Fatigue campaign

Our test campaign:

- 4T sub-rope
- R ratio close to zero
- Fmin fixed and varying Fmax



Conclusions:

- Linear trend observed for the 4T tested load ranges

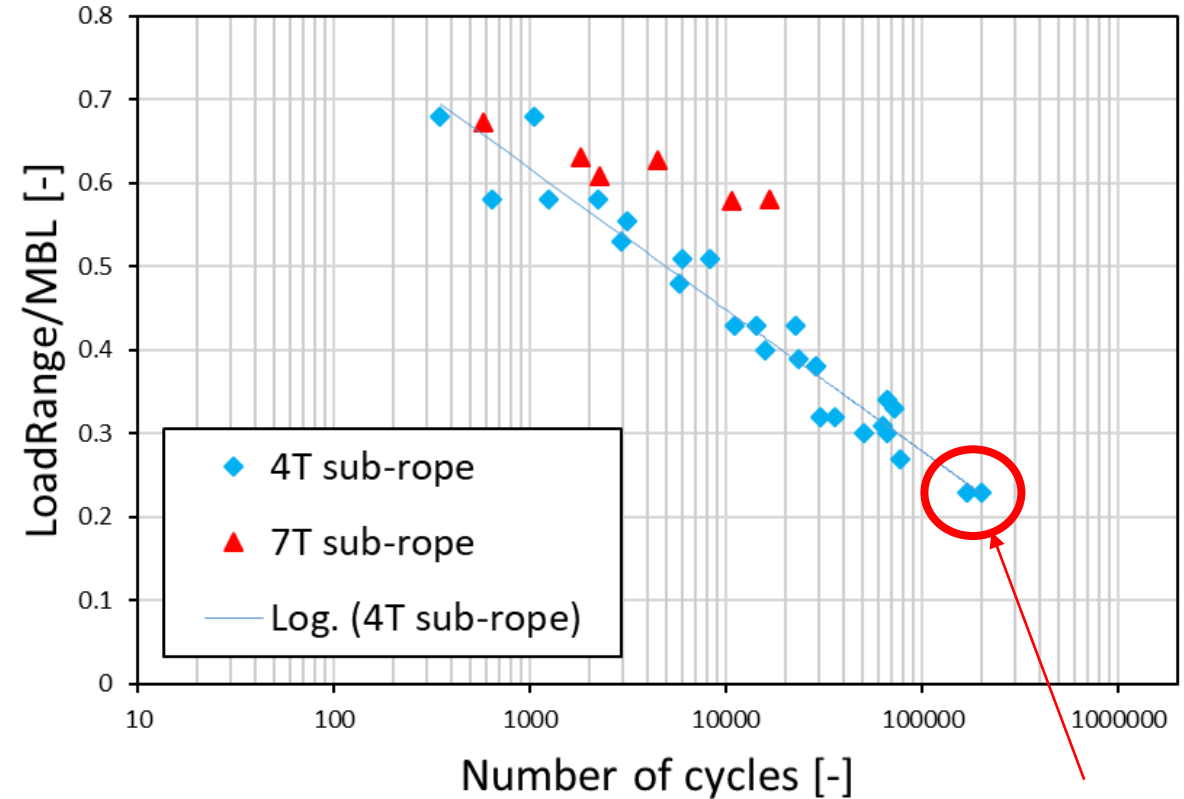
Fatigue campaign

Our test campaign:

- 4T sub-rope
- R ratio close to zero
- Fmin fixed and varying Fmax

Chevillotte 2020:

- 7T sub-rope
- R ratio close to zero



1-month tests

Conclusions:

- Linear trend observed on semi-log plot for the 4T tested load ranges
- The smaller lay-length impacts the fatigue lifetime
- The results obtained with the 4T scale sub-rope are close to the results for more realistic constructions

Fatigue campaign

Our test campaign:

- 4T sub-rope
- R ratio close to zero
- Fmin fixed and varying Fmax

Chevillotte 2020:

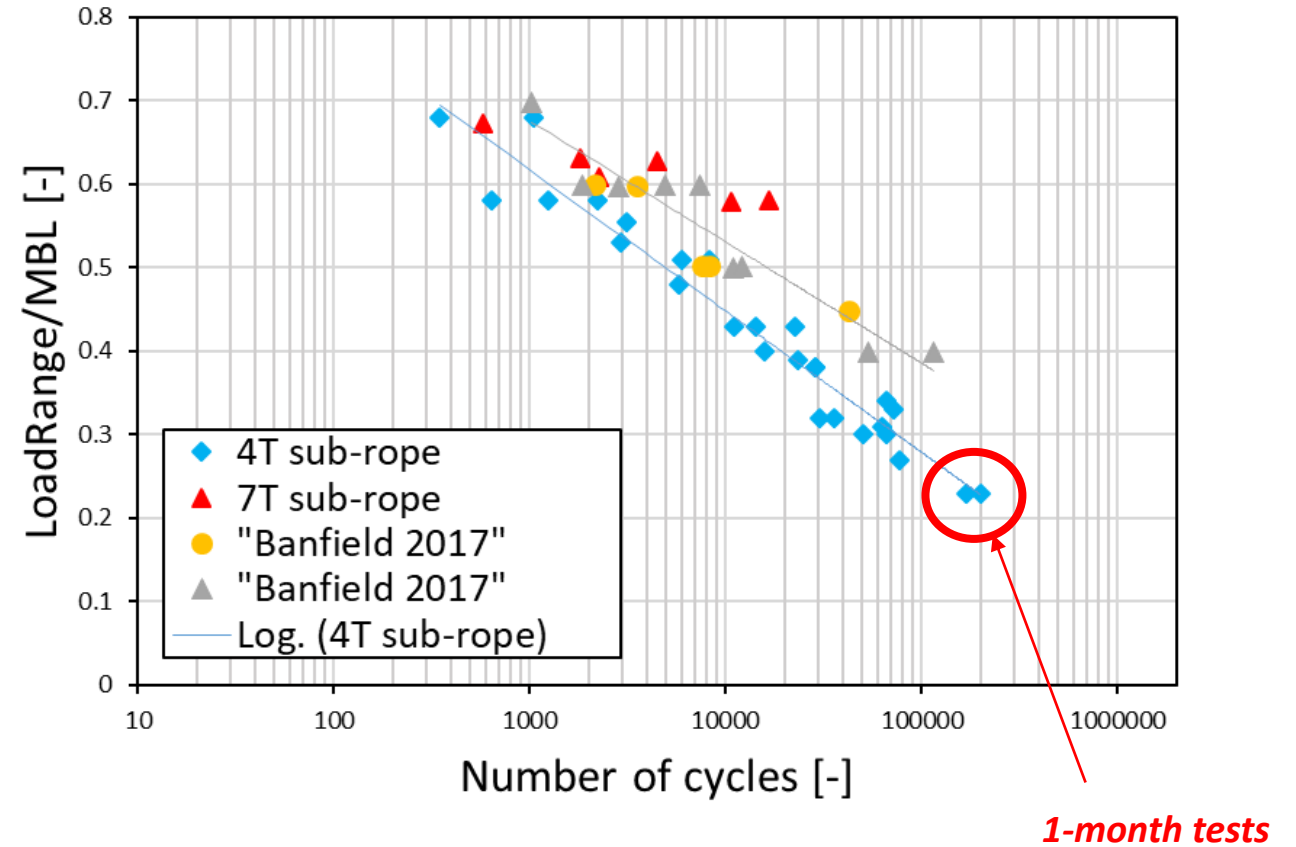
- 7T sub-rope
- R ratio close to zero

Banfield 2017:

- Twisted polyamide sub-ropes with two constructions.
- R ratio varying between 0.3 and 0.5

Conclusions:

- Linear trend observed for the 4T tested load ranges
- The smaller lay-length impacts the fatigue lifetime
- The results obtained with the 4T scale sub-rope are close to the results for more realistic constructions



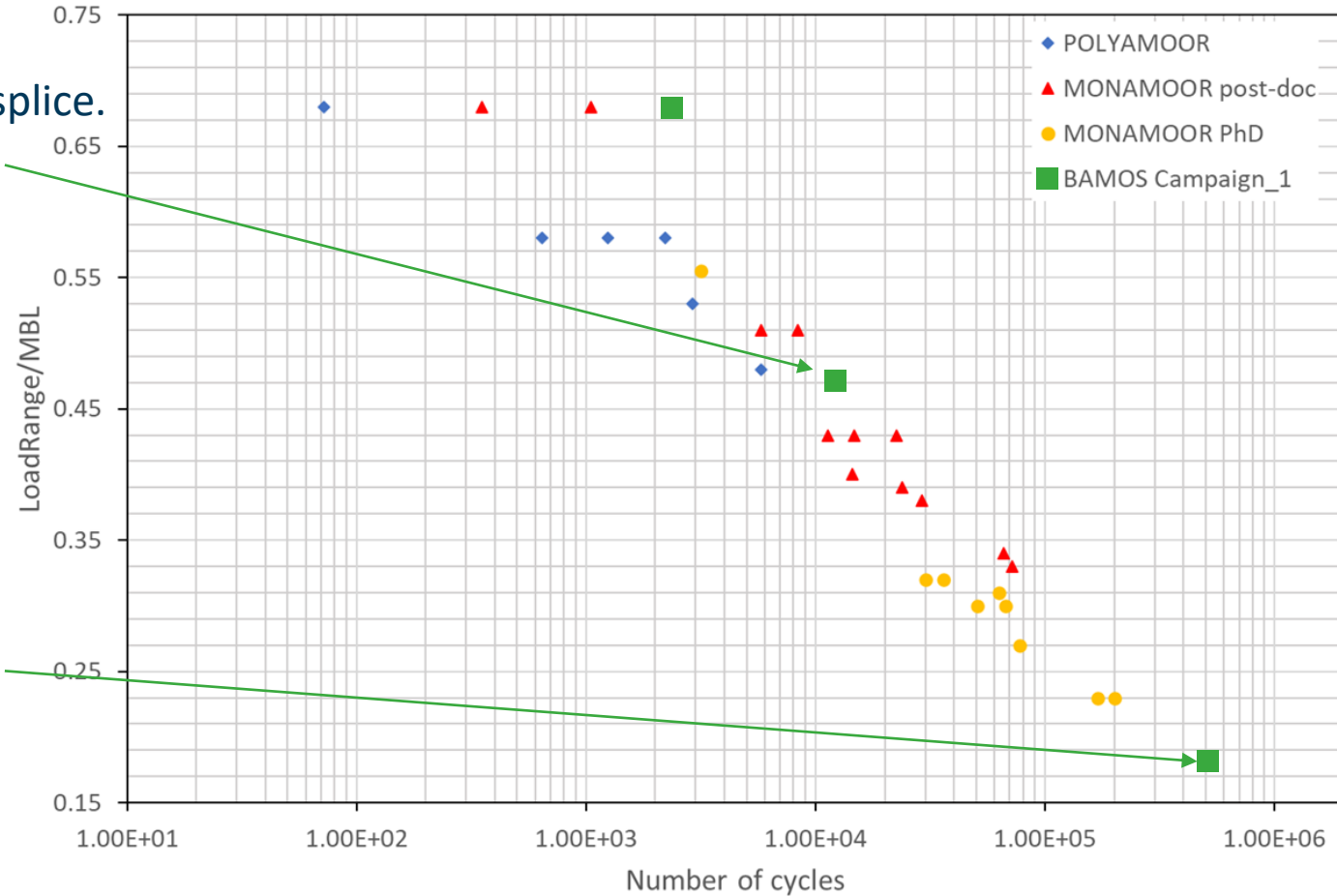
Fatigue campaign: on-going project



Failure in the eye's splice.
Conservative result

Interrupted test.
Conservative result

70%MBL 49%MBL 20%MBL



Tomography study on aged rope

Studied specimens

Sample after 29 %MBL
fatigue test



Virgin sample



Experimental set-up

- Polyacetal container
- One lay pitch can be scanned
- Tension 400 N



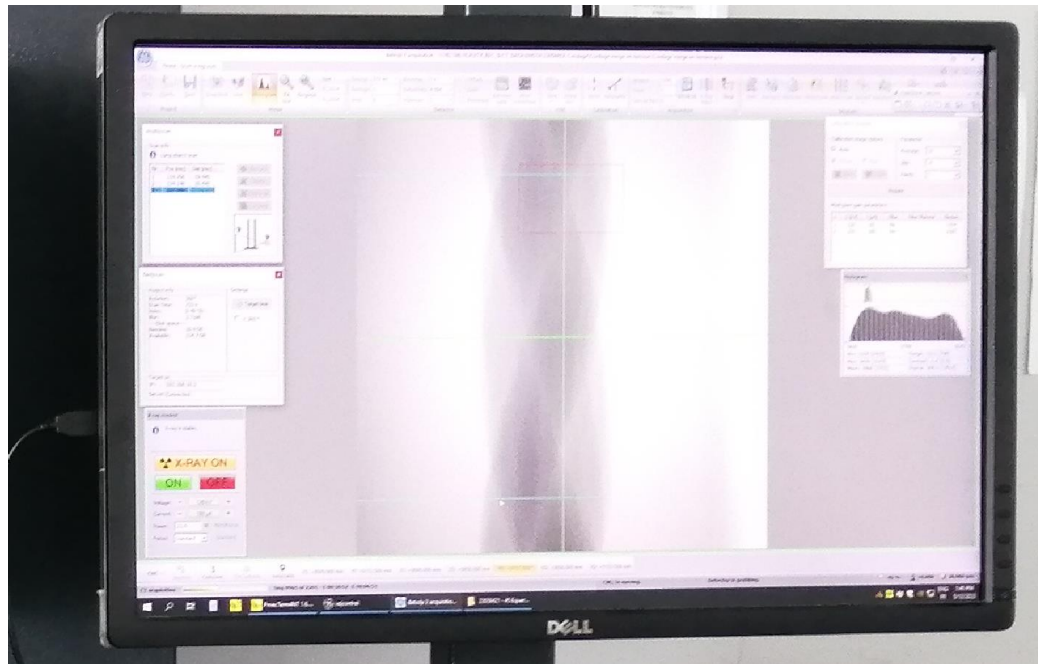
Tomography: experimental set up

Tomography at CRT Morlaix.

Higher resolution available: 20 μm .

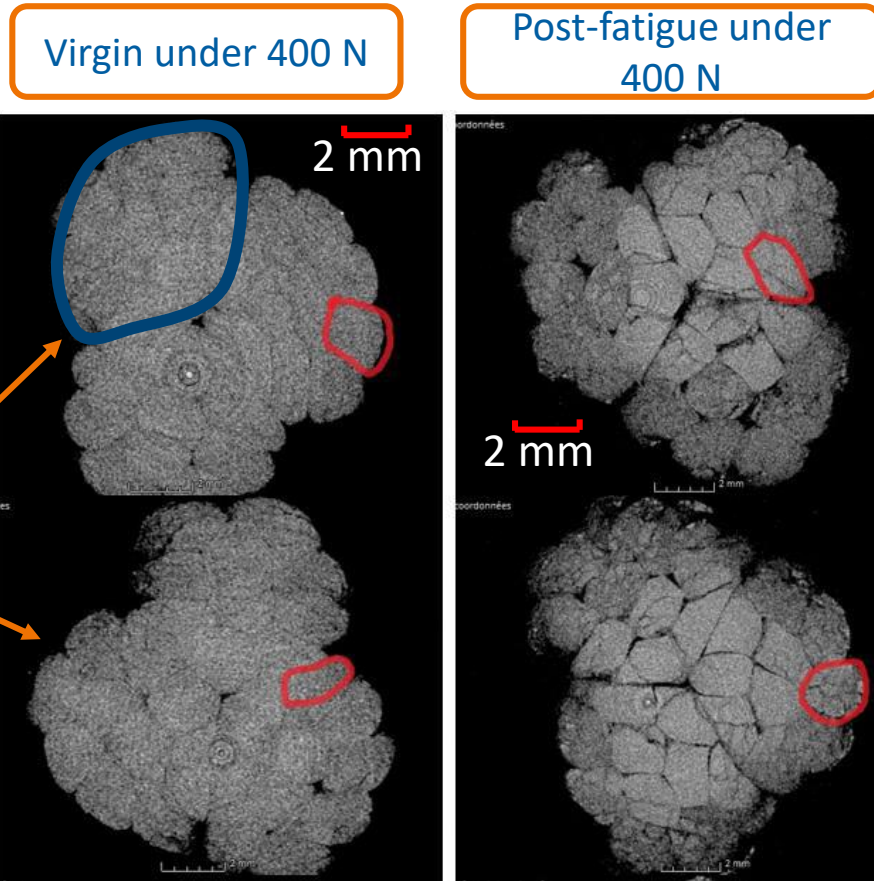
3 scans with 2200 pictures per scan

Total time of a tomography: 45 minutes



Tomography results: virgin/aged

Higher resolution available: 20 μm .



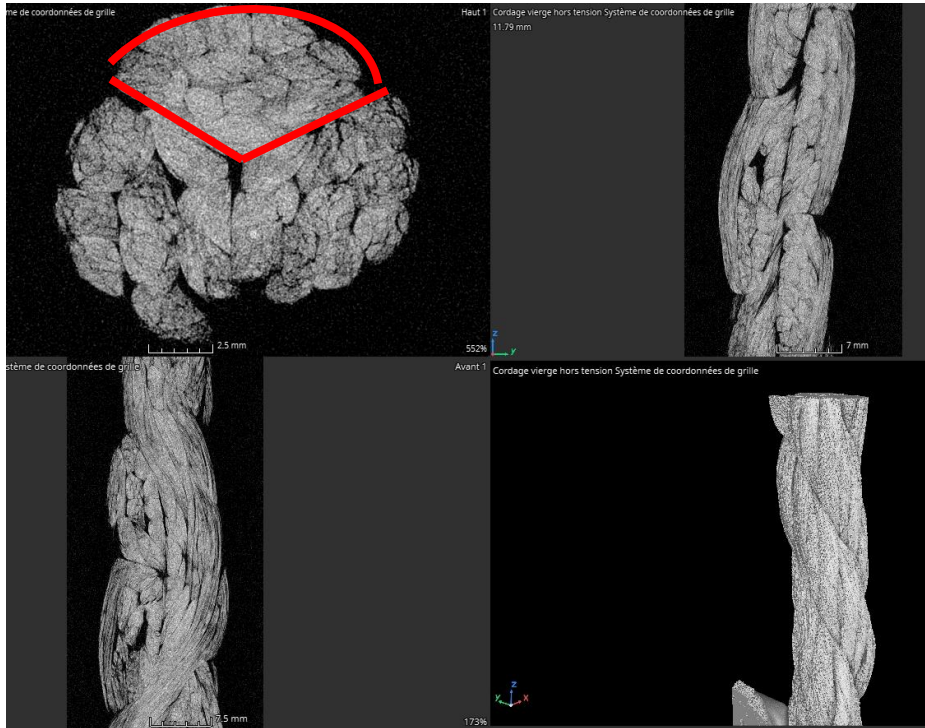
Observations on the post-fatigue sample:

- Gradient of compaction inside the sub-rope
- Rope-yarns shape very angular
- Contact area very visible

Tomography results: virgin/aged

Virgin under 400 N

1 strand: 10 rope-yarns



No tension

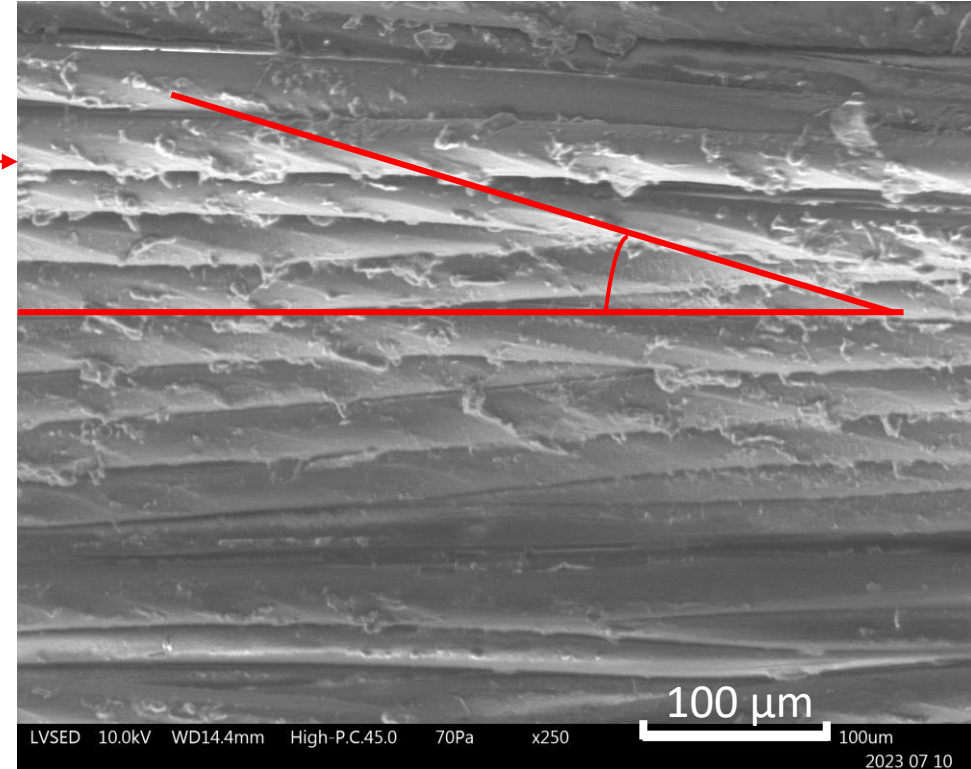
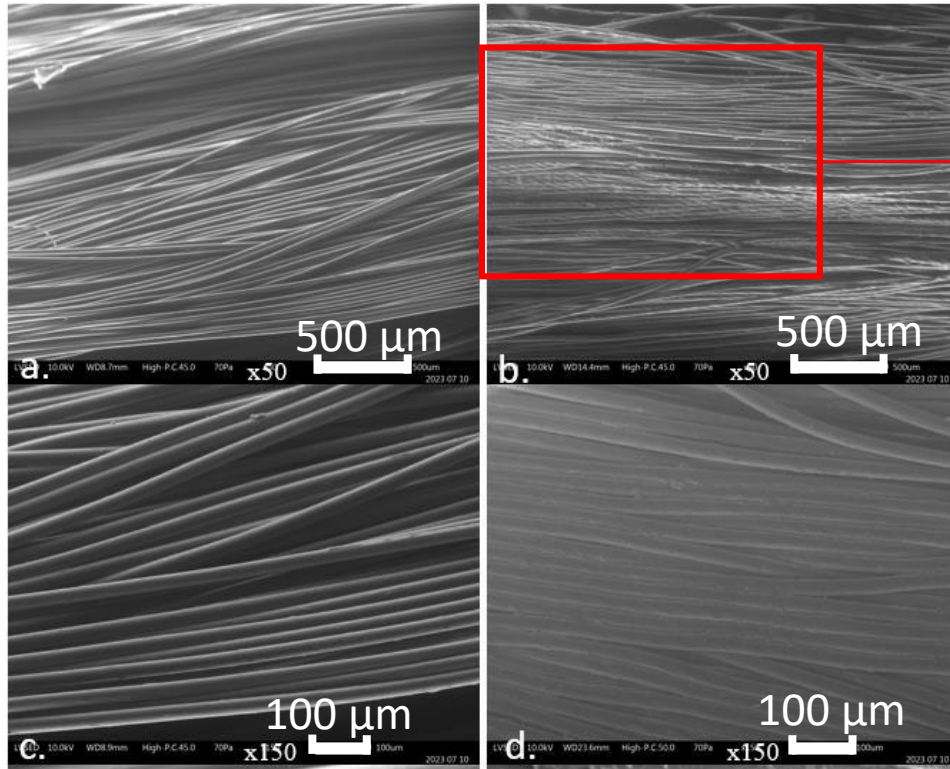
Post-fatigue under 400 N



SEM results aged/virgin

Virgin

Post-fatigue



Observations on the post-fatigue sample:

- The filaments are more compacted and aligned

Observations on the zoom:

- Marks are due to the friction with the fibres in contact
- Friction coefficient will depend on the direction of the fibres

Fatigue study: conclusion and perspectives

Fatigue:

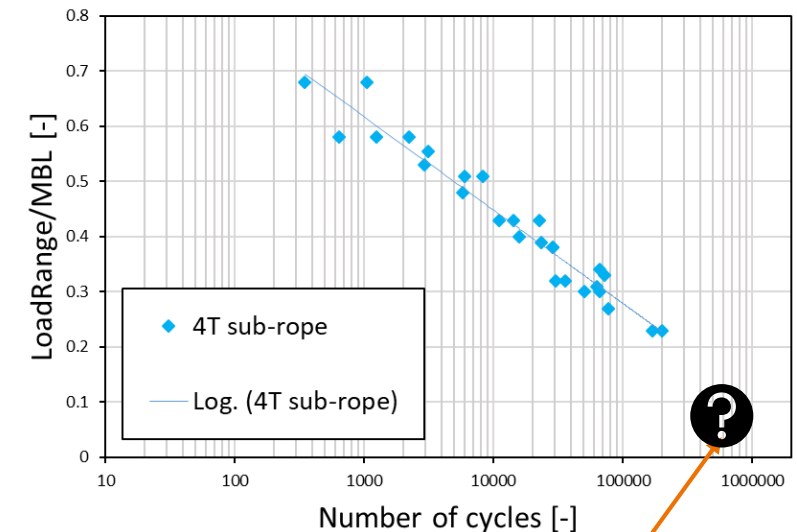
- S-N curve extended to 10^5 cycles on 4T sub-ropes
- The 4T construction is interesting to investigate fatigue: conservative and easier to study

Damage analysis:

- New state and organisation of the material at the rope-yarns scale:
 - More compact
 - Fibres more aligned
- The rope-yarns are sharper

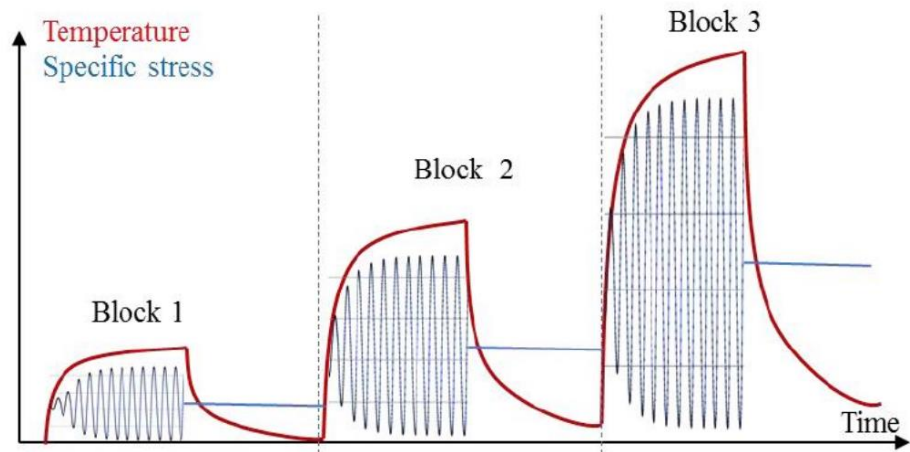
How to speed-up the characterization of the fatigue curve ?

Additional study and perspectives: self-heating method



Self-heating for fast fatigue prediction

The self-heating method applied on sub-ropes



Several phenomena:

- Thermo-elastic coupling
- Inherent elevation of temperature due to potential damaging mechanisms

The global dissipation per cycle:

$$\Delta^* = \frac{\theta_{MAX}}{f_r \times \tau_d}$$

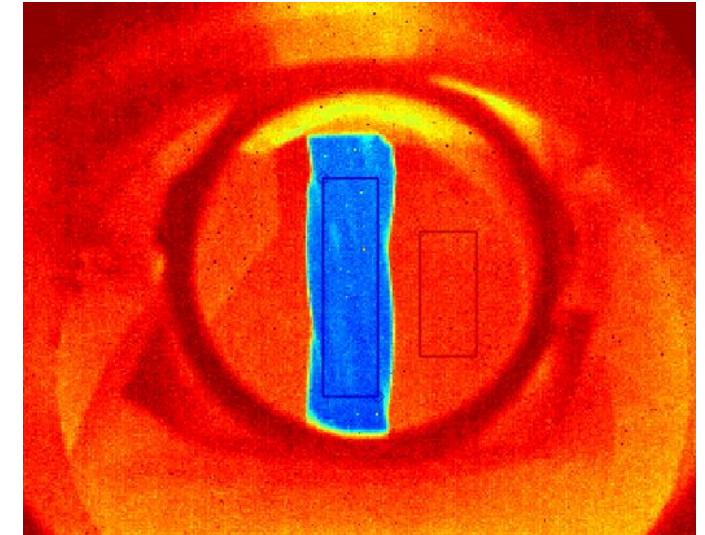
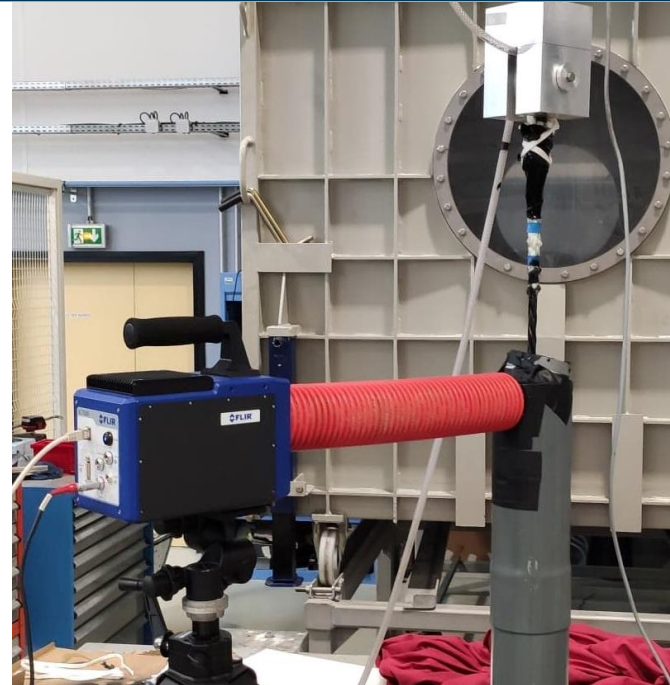
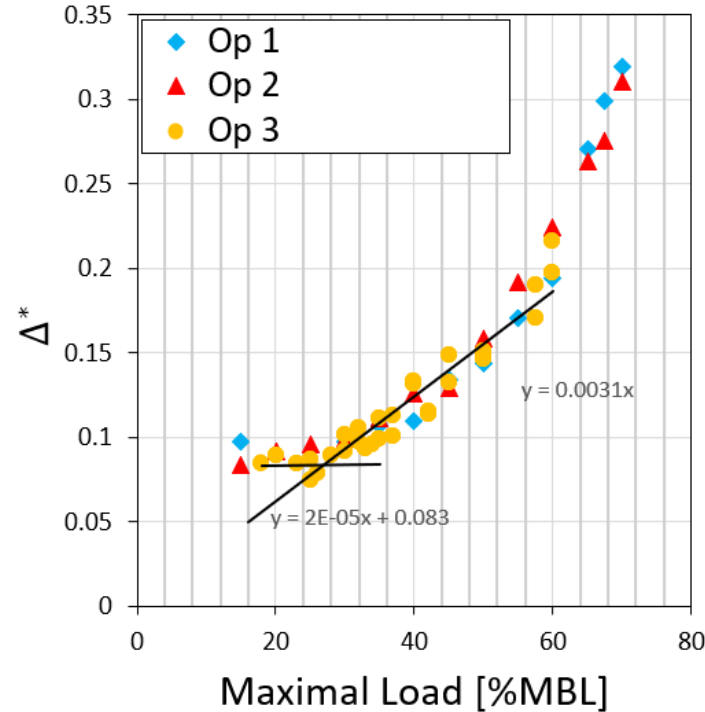
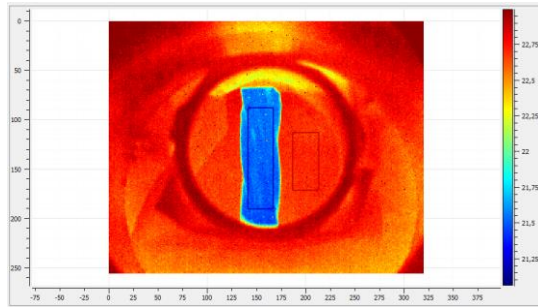
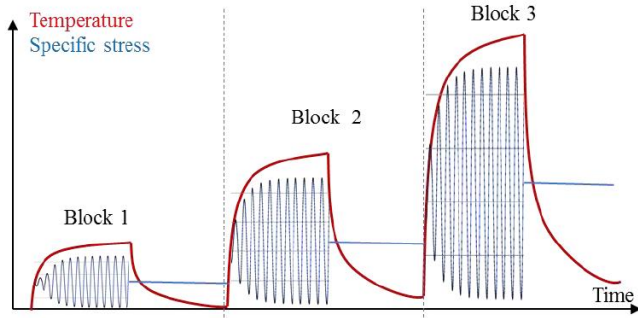


Image from Célénos software (Le Saux, V. (2023))

Motivations:

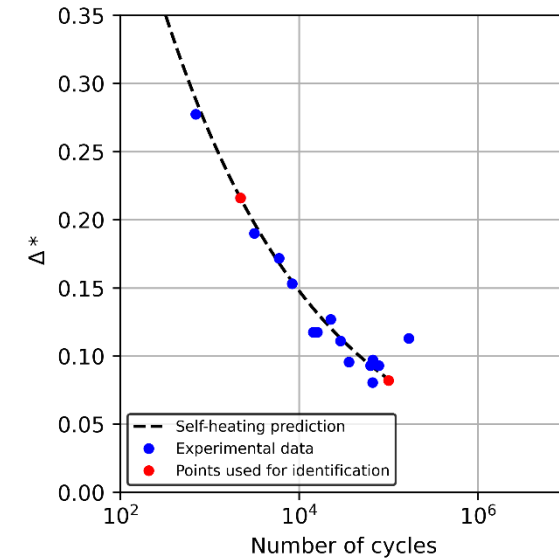
- Link mechanisms and energy conversion to **damage and failure scenarios**
- Understand the **dissipation mechanisms**: $\Delta^*_{material} + \Delta^*_{friction}$

The self-heating method applied on sub-ropes



Use of an energy criteria to predict fatigue life:

$$\Delta^* N^b = C$$

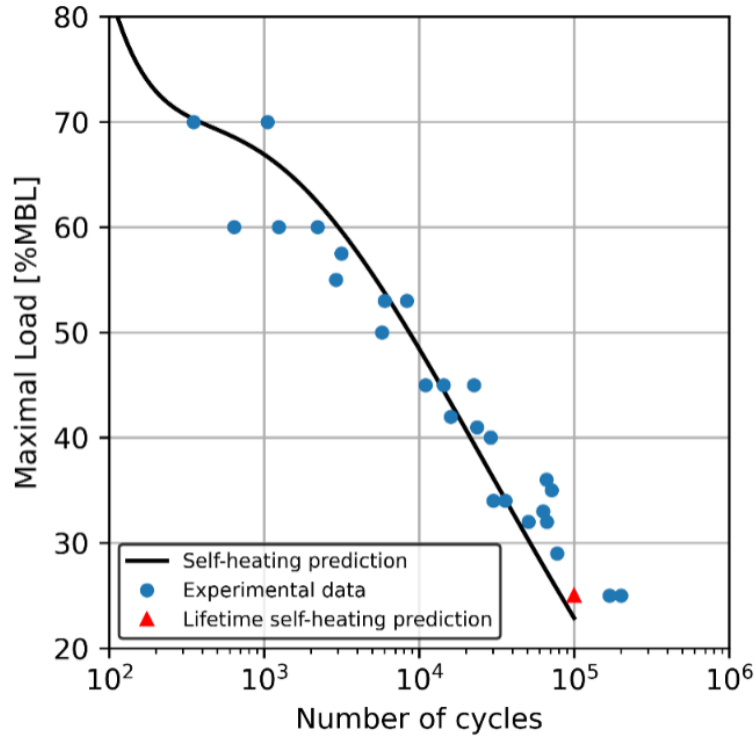


The global dissipation per cycle:

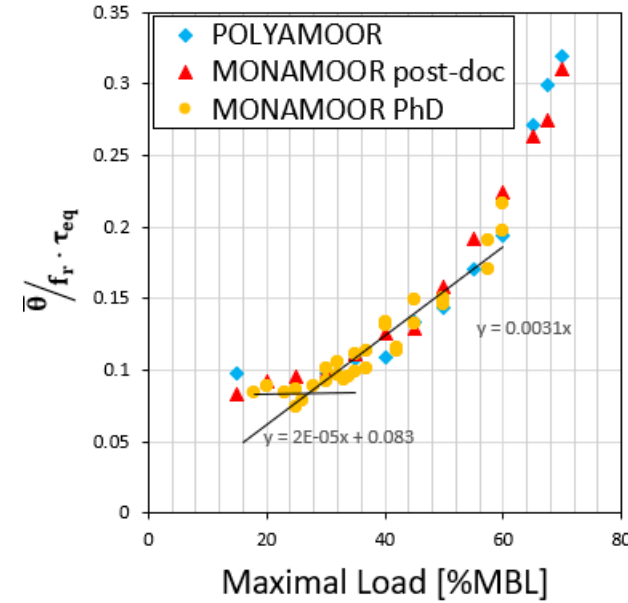
$$\Delta^* = \frac{\theta_{MAX}}{f_r \times \tau_d}$$

Mechanisms and energy conversion ↔ Damage and failure scenarios

The self-heating method applied on sub-rope

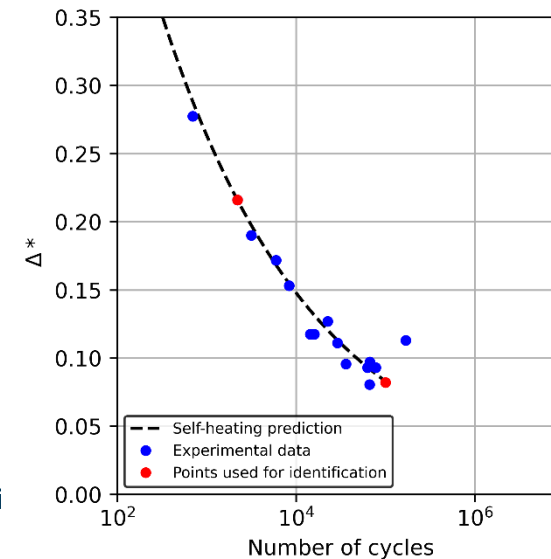


Obtention of a fatigue curve based on an energy criteria



New graphical determination of regime

Need to overcome the graphical approach



Improved identify energy criteria

Self-heating method: to perform fast characterization of the S-N curve for ropes

- ✓ Repeatability of the self-heating protocol validated
- ✓ Graphical fatigue prediction performed

→ Need of a model **to understand the dissipation mechanisms**: $\Delta_{material}^* + \Delta_{friction}^*$

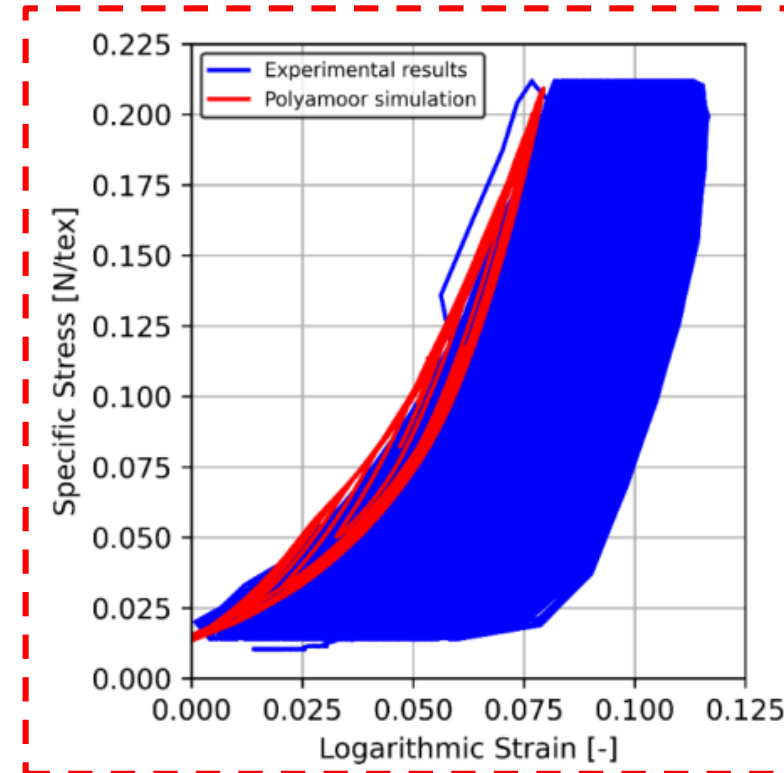
→ **Fatigue prediction method for PA ropes using self-heating approach, to better understand the internal dissipation mechanisms for different load ratios**

Heat build-up protocol applied to higher scale sub-ropes

Heat build-up protocol to catch the influence of the load ratio on the fatigue properties

L.Civier, Y.Chevillotte, C.Bain, G.Bles, Y.Marco, P.Davies - Fatigue study of twisted polyamide sub-rope for floating wind turbines: Fast evaluation with heat build-up protocol and tomography study of mechanisms, Ocean Engineering (2024)

- On the influencing parameters of PA ropes fatigue
- Challenge of a new fatigue criterion for synthetic ropes



Questionable: only one test !



I. France Energies Marines institute

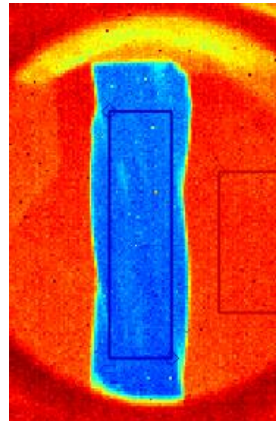
II. Industrial context

III. Behavior law for mooring design

IV. Study of fatigue lifetime

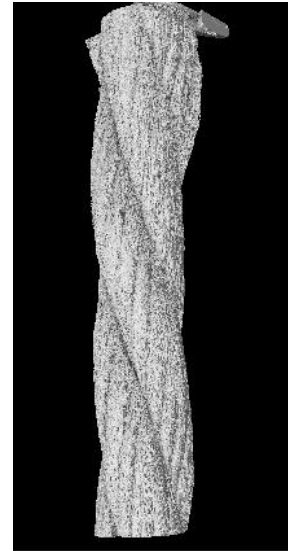
V. Multi-scale modeling

Development of a multi-scale model



- Predict the impact of the construction parameter on the behavior/rigidity (strands diameter, lay-length, number of strands...)
- Understand the friction/abrasion

Multi-scale model



3D multi-scale model

Constitutive behaviour

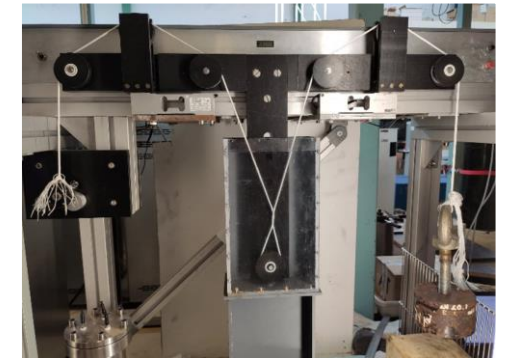
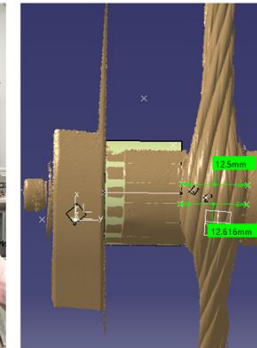
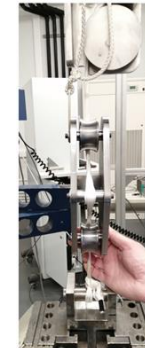


Friction

$\Delta^*_{material}$

$\Delta^*_{friction}$

Measurements

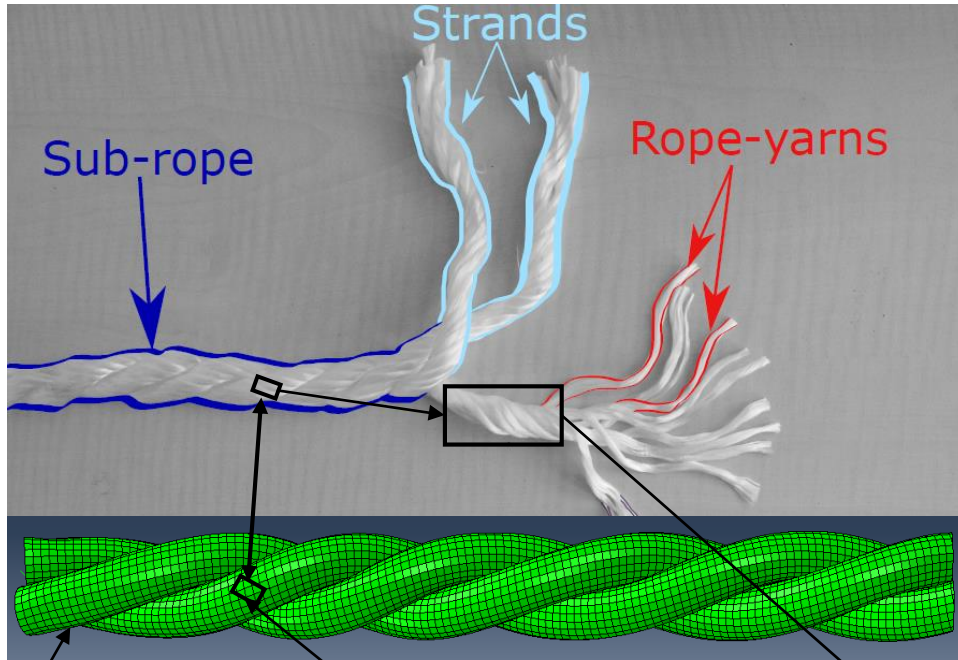


Procedure followed:

- Choice of a scale and approach
 - Theoretical development
 - Identification
 - Validation



First definition of the law with hyper-elastic potential: no dissipation in the friction modes and no visco (elasto-plasticity).



3 cylinders in contact

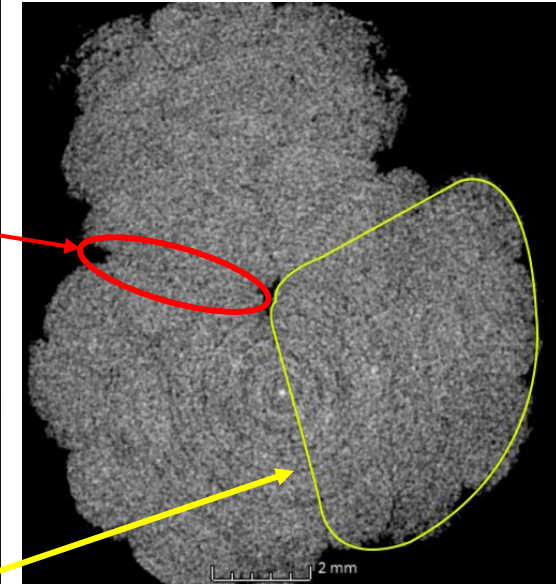
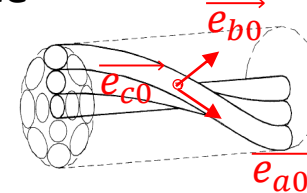
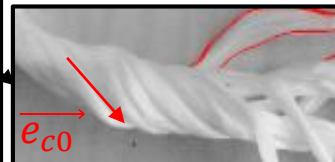
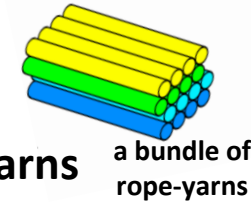
A behaviour law in all the integration points

Strands Scale:

- 3 cylinders in contact
- Geometries
- Surfaces
- Inter-strand friction

Rope-yarns scale:

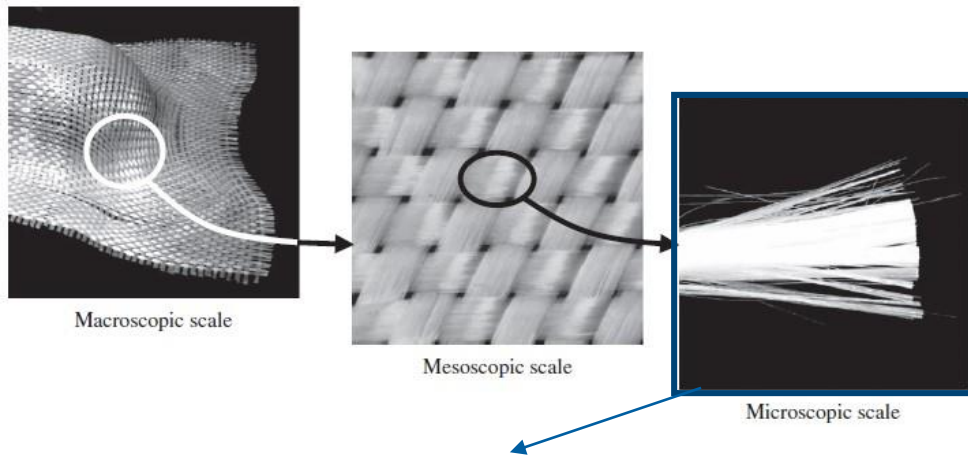
- A behaviour law
- Friction between rope-yarns (intra-strand frictions)
- Visco-elasto-plasticity
- Change of volume



Which behaviour law ?

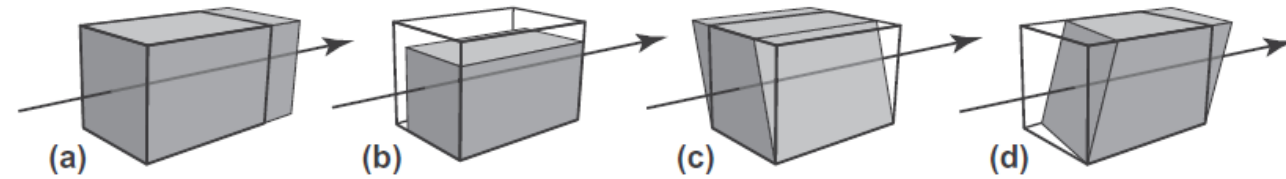
Chosen approach

Charmetant *et al.* 2011. A. Charmetant approach developed for the mechanical behaviour of textile composite reinforcements :



Anisotropic hyperelastic model:

- Homogeneous material corresponding to a bundle of fibres
- Material considered transversely isotropic
- Null intrinsic dissipation

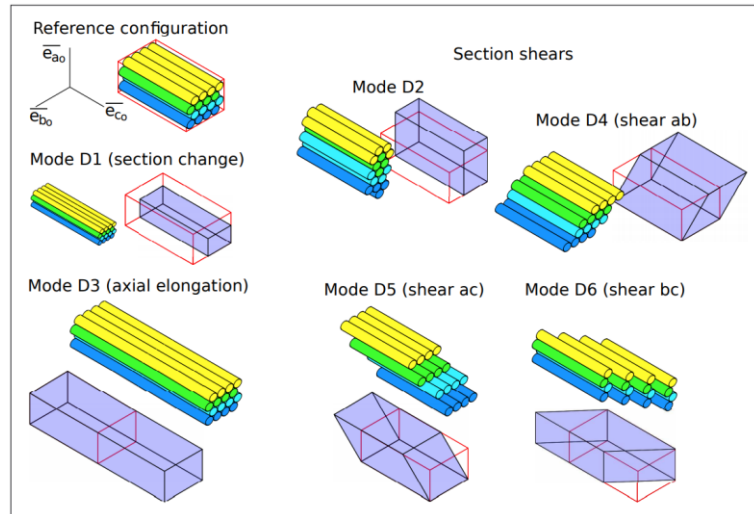


- Deformation decomposition valid in large deformation
- Choice of four scalar invariants strain-physically based to describe each deformation mode
- Choice of dedicated behaviour law for each deformation mode

Charmetant choice of invariants: Limited description of the shear strain modes

Adaptation of Charmetant's approach to completely describe the shear modes: **development of the FiBuLa law**

(fibre bundle law)



In small deformation, all deformation can be decomposed in 6 deformations modes:

$$\tilde{E} = \varepsilon_1 \tilde{D}_1 + \varepsilon_2 \tilde{D}_2 + \varepsilon_3 \tilde{D}_3 + \varepsilon_4 \tilde{D}_4 + \varepsilon_5 \tilde{D}_5 + \varepsilon_6 \tilde{D}_6$$

With the set of tensor \tilde{D}_i an orthonormal basis of the vector space of the second-order symmetric tensors.

$$\tilde{D}_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}_{(\tilde{e}_{io})}$$

$$\tilde{D}_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix}_{(\tilde{e}_{io})}$$

$$\tilde{D}_3 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}_{(\tilde{e}_{io})}$$

$$\tilde{D}_4 = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}_{(\tilde{e}_{io})}$$

$$\tilde{D}_5 = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix}_{(\tilde{e}_{io})}$$

$$\tilde{D}_6 = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}_{(\tilde{e}_{io})}$$

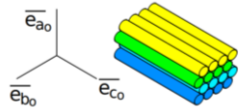
- **The longitudinal shears:** $(\varepsilon_5 \tilde{D}_5 + \varepsilon_6 \tilde{D}_6)$

- **The transverse shears:** $(\varepsilon_2 \tilde{D}_2 + \varepsilon_4 \tilde{D}_4)$

→ Deformation decomposition valid in large deformation

→ Choice of invariants that describe completely the 6 strain modes

Deformation decomposition



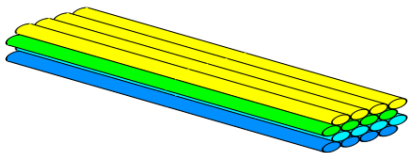
\tilde{F} is the deformation gradient tensor to pass from the initial configuration Ω_0 to the current configuration Ω

$$\tilde{F} = \tilde{R}_\pi \circ \tilde{U}_c \circ \tilde{U}_{vol} \circ \tilde{U}_{ab} \circ \tilde{K}_\pi^{-1}$$

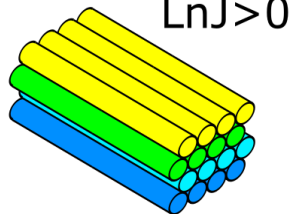
Rope-yarns behaviour (deformation mode without shear)

Friction (shear deformation modes ($\tilde{U}_{ab}, \tilde{K}_\pi^{-1}$))

\tilde{U}_c



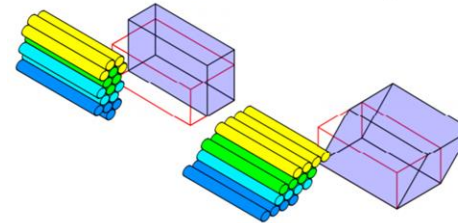
\tilde{U}_{vol}



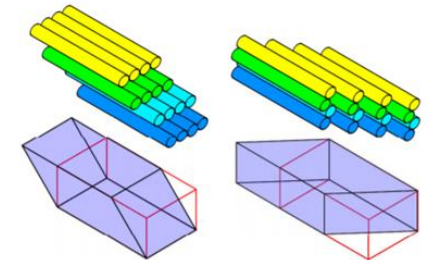
$$\ln U_c = \ln\left(\frac{1}{\sqrt[3]{J}} \frac{c}{c_0}\right)$$

$$\ln J = \ln(\det \tilde{F})$$

\tilde{U}_{ab}



\tilde{K}_π^{-1}



$$\ln \tilde{U}_{ab} = \begin{bmatrix} \ln U_{ab11} & \ln U_{ab12} & 0 \\ \ln U_{ab12} & -\ln U_{ab11} & 0 \\ 0 & 0 & 0 \end{bmatrix}_{(\bar{e}_{i0})}$$

$$\tilde{\varepsilon}_\delta = \begin{bmatrix} 0 & 0 & \delta_a/2 \\ 0 & 0 & \delta_b/2 \\ \delta_a/2 & \delta_b/2 & 0 \end{bmatrix}_{(\bar{e}_{i0})}$$

Obtention of the stress-strain FiBuLa law

Free specific energy:

$$\forall(\theta, \tilde{F}) \psi(\theta, \ln J, \ln Uc, \widetilde{Ln U}_{ab}, \widetilde{\varepsilon}_\delta) = W_{Jc}(\theta, \ln J, \ln Uc) + W_{ab}(\theta, \widetilde{Ln U}_{ab}) + W_\delta(\theta, \widetilde{\varepsilon}_\delta)$$

Thermodynamic



$$\forall(\theta, \tilde{F}, \tilde{D}) \tilde{\Sigma} : \tilde{D} = W'^J_{Jc} \cdot \dot{\ln J} + W'^c_{Jc} \cdot \dot{\ln Uc} + \widetilde{W}'_{ab} : \dot{\widetilde{Ln U}_{ab}} + \widetilde{W}'_\delta : \dot{\widetilde{\varepsilon}}_\delta$$

with $\widetilde{W}'_a = \frac{\partial \widetilde{W}_a}{\partial \tilde{X}}(\theta, \tilde{X})$; $W'_a{}^x = \frac{\partial W_a}{\partial x}(\theta, x, y)$ and $W'_a{}^y = \frac{\partial W_a}{\partial y}(\theta, x, y)$

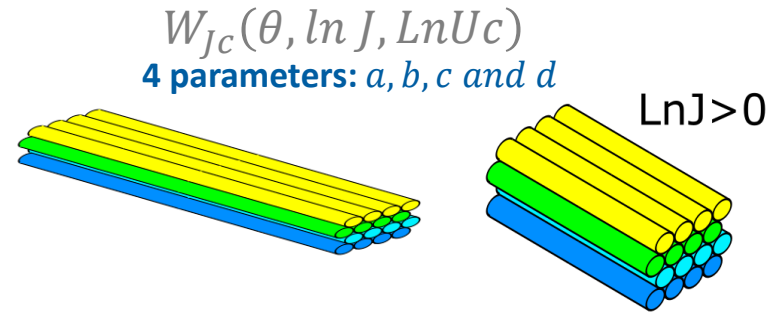
Algebra



Stress-Strain law:

$$\forall(\theta, \tilde{F}) \widetilde{R}_\pi^T \cdot \tilde{T} \cdot \widetilde{R}_\pi = \dots$$

Identification of the axial elongation and change of volume mode



Specifications:

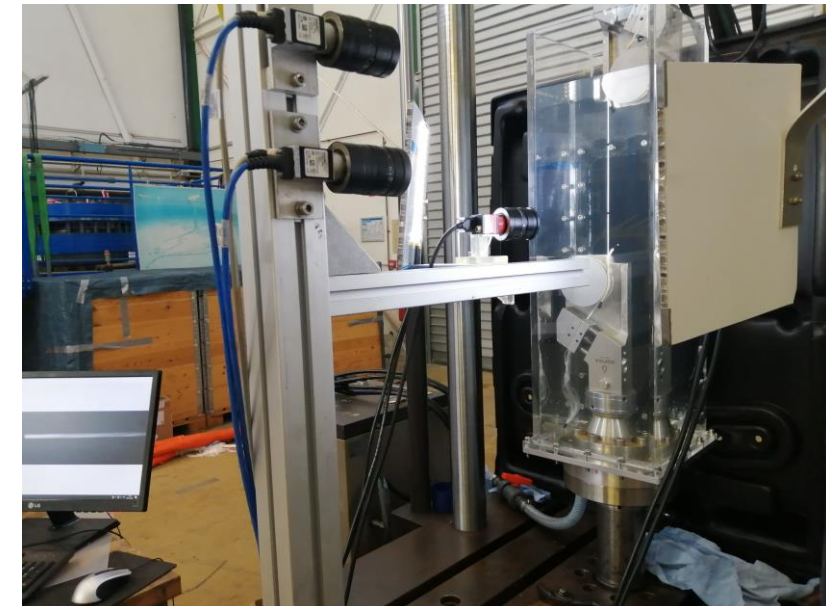
- Test rope-yarns and strand
- Adapted terminations to distribute the load
- Test in water
- Monitoring of the axial and transversal strain

Experimental set-up:

- Capstan grips
- A rectangular tank full of water
- 2 cameras to measure the axial elongation
- 1 camera to measure the transversal strain
- 1 year of development



Capstan grips

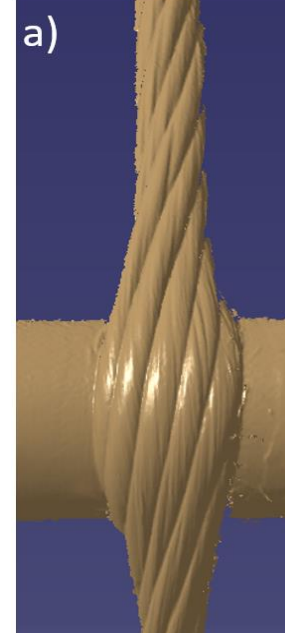
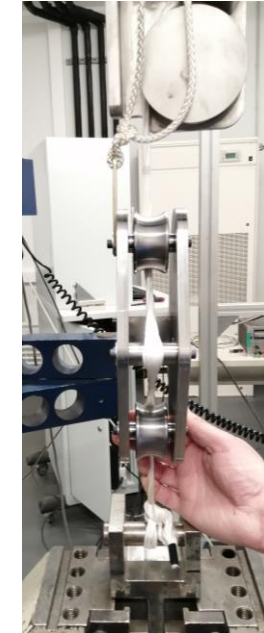
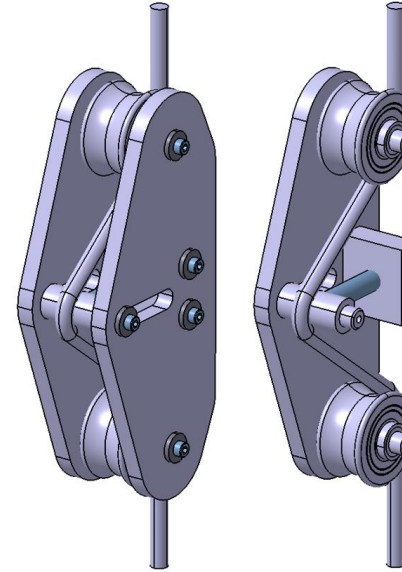
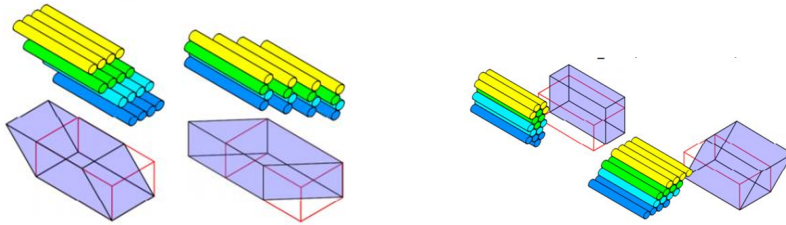


Experimental set-up

Experimental Identification of the shear strains modes

$$W_{ab}(\theta, \ln \bar{U}_{ab}) \text{ and } W_{\delta}(\theta, \bar{\varepsilon}_{\delta})$$

2 parameters: G_{ab} and G_{δ}



Specifications:

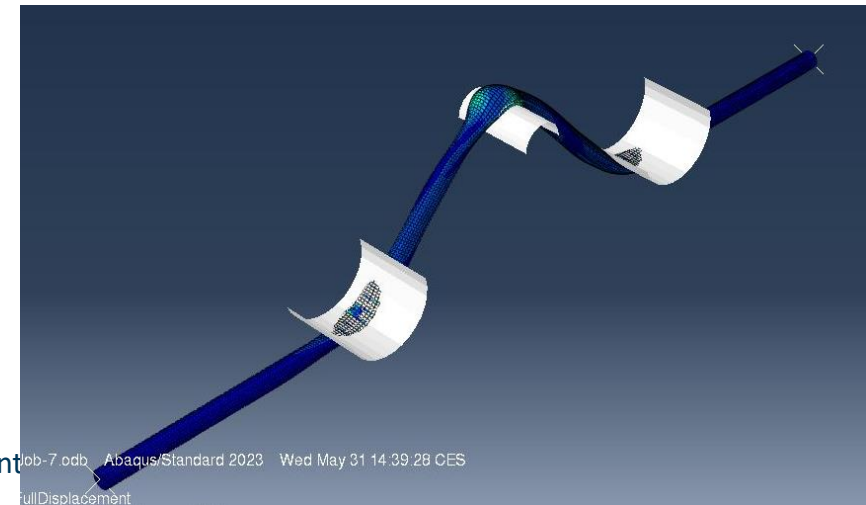
- Test a strand in the configuration « contact with a rod »
- Use the adequate monitoring to measure the contact between the rod and the strands

Experimental set-up:

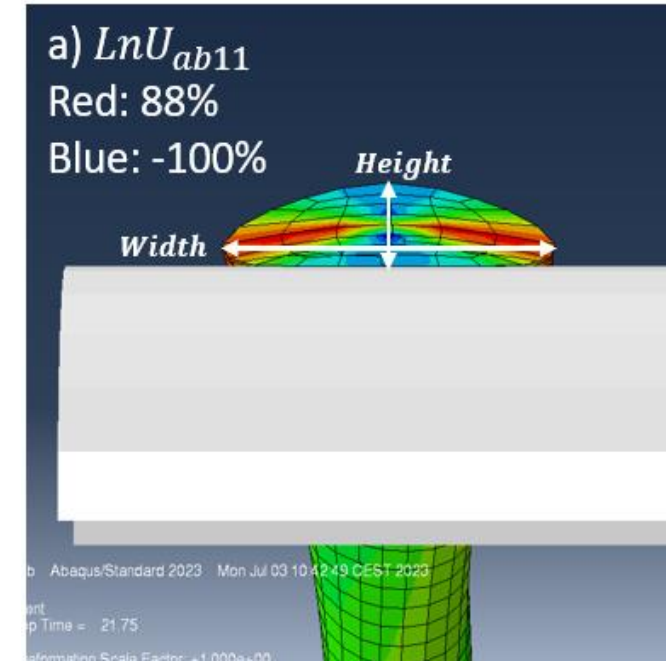
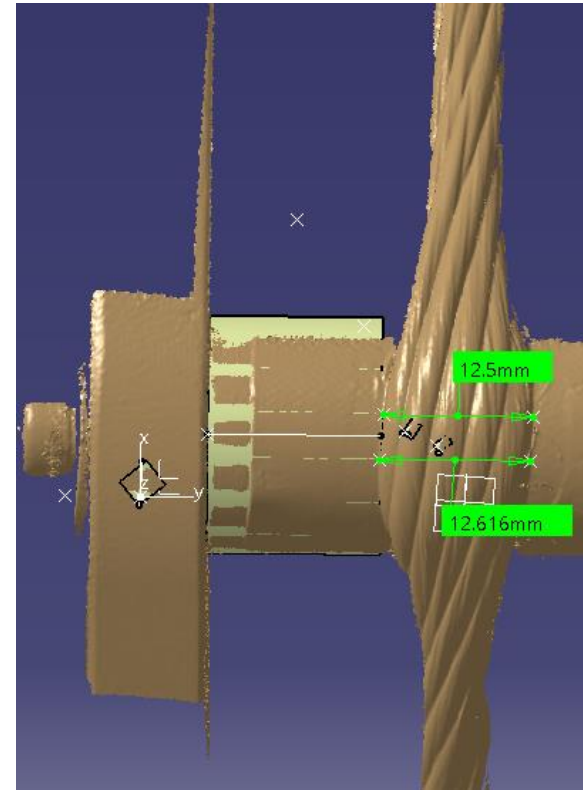
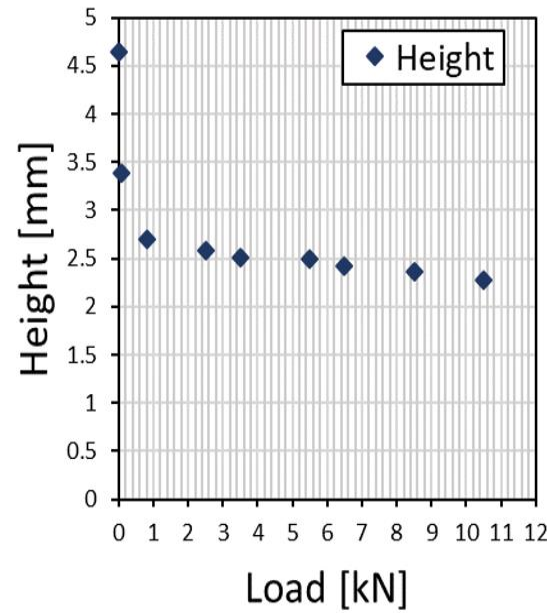
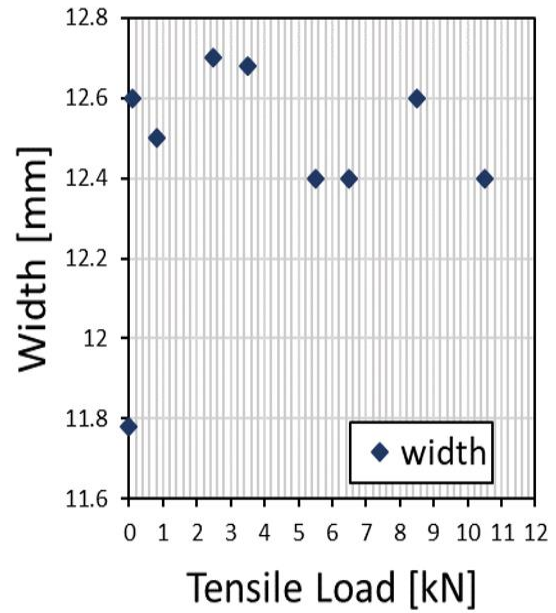
- '3-rod' device conceived
- Tensile test with interruption each 2000 N
- 3D scan of the contact area

- 6 months of development

Inverse identification using the software Abaqus



Identification of the shear strains modes

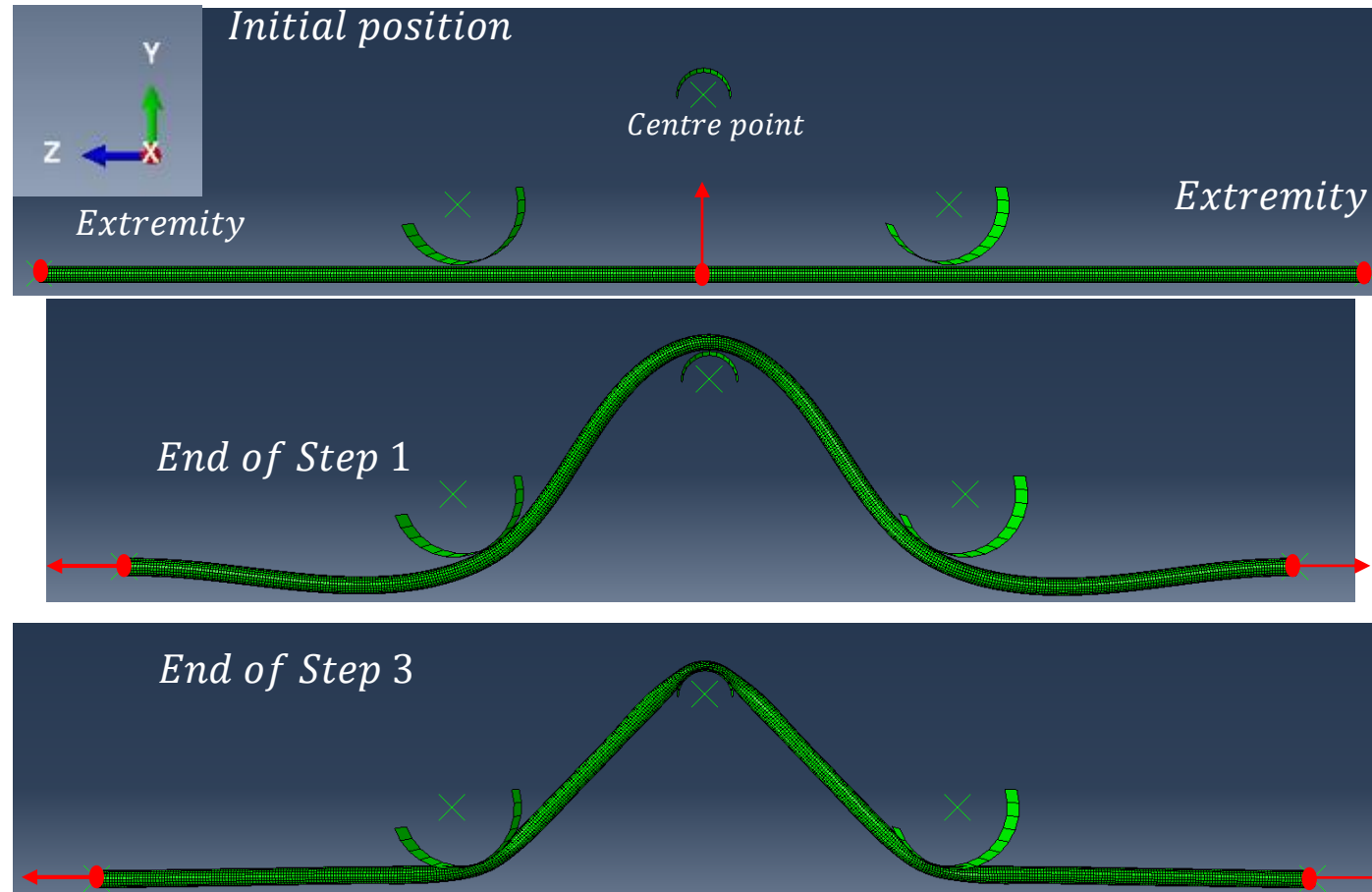


Strategy used:

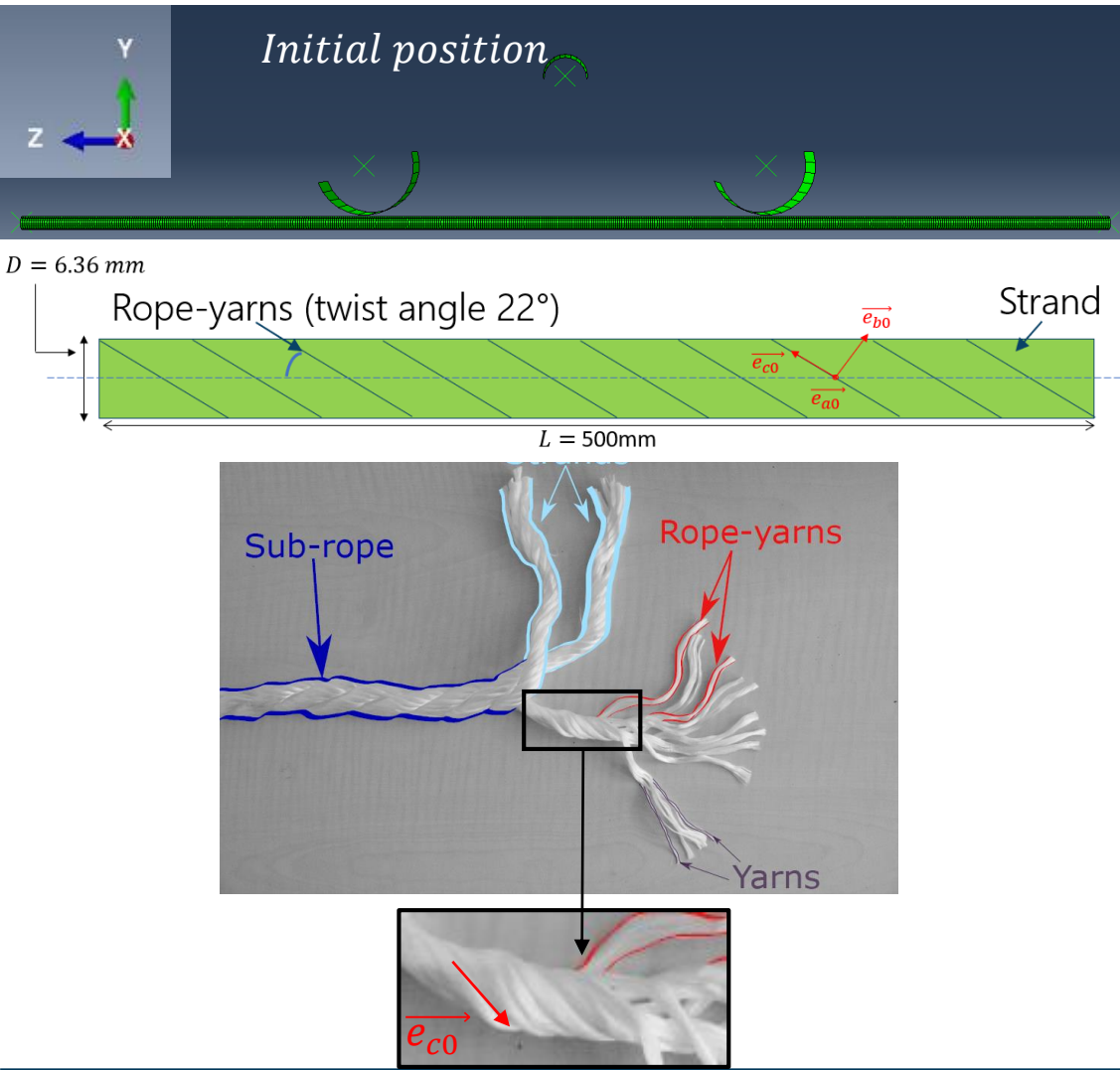
Measurement of height and width every 2000 N during the tensile test

Simulation: Diametral Compression

- Implementation of the FiBuLa law on a UMAT for its use Abaqus™ software/Standard (Implicit algorithm)
- Three steps in Abaqus/Standard (Implicit algorithm) and 22000 cubic elements (C3D8)



Simulation: A Diametral Compression



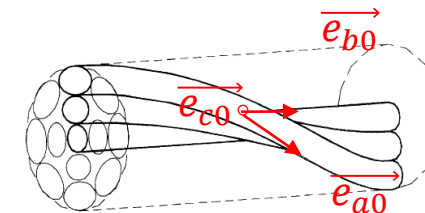
A parameter of the FiBuLa law:

- A point on the helix axis of the strand

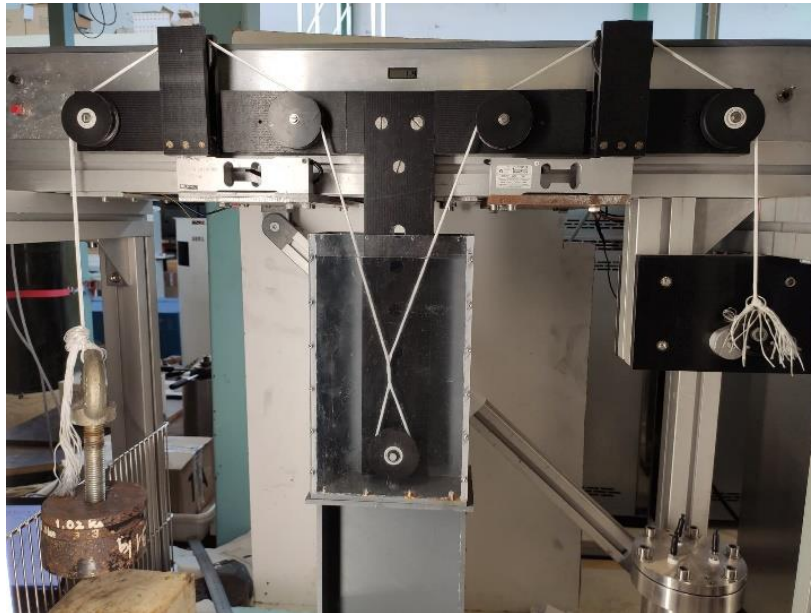
Behaviour law implemented in each integration points:

- Determination of the position of the integration points regarding the point on the helix axis
- Calculation of the rope-yarn orientation using Leech (2002) description:

$$\cos\alpha_{RY} = \frac{1}{\sqrt{1 + (2 \cdot \pi \cdot p \cdot r_{RY})^2}}$$

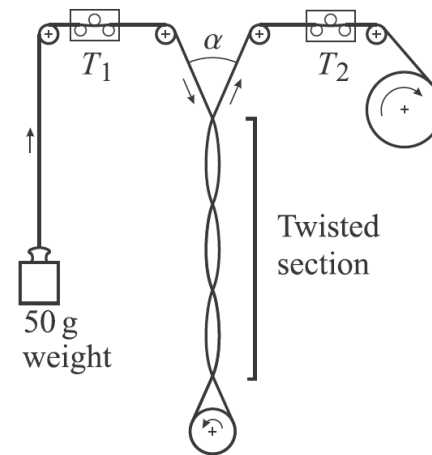


Characterization of one parameter: the friction coefficient



ASTM D3412-0 (γ small) type B. Cornelissen et al. (2013)

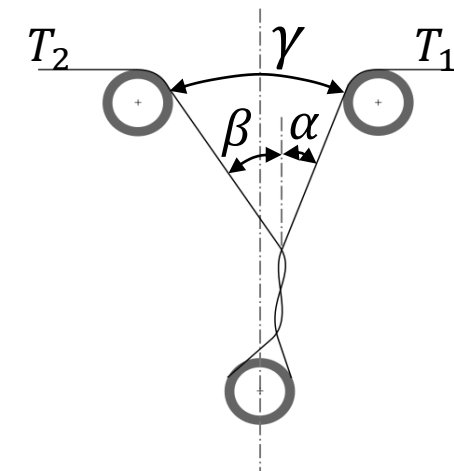
Symmetrical problem



$$\mu = \ln\left(\frac{T_1}{T_2}\right) \frac{1}{2\pi n \gamma}$$

Hobbs analysis (2018):

No symmetry because $T_1 > T_2$

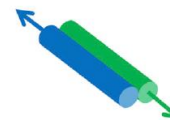


$$\mu = \frac{(T_1 - T_2) \tan(\gamma/2)}{\pi(N_c - 1)(T_1 \sin^2 \alpha + T_2 \sin^2 \beta)}$$

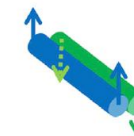


- Experimental test bench for friction test: rope yarn on rope yarn at IFREMER, Brest

In literature, at filament scale (Gassara et al, 2018) : $\mu_l \approx 0,25$

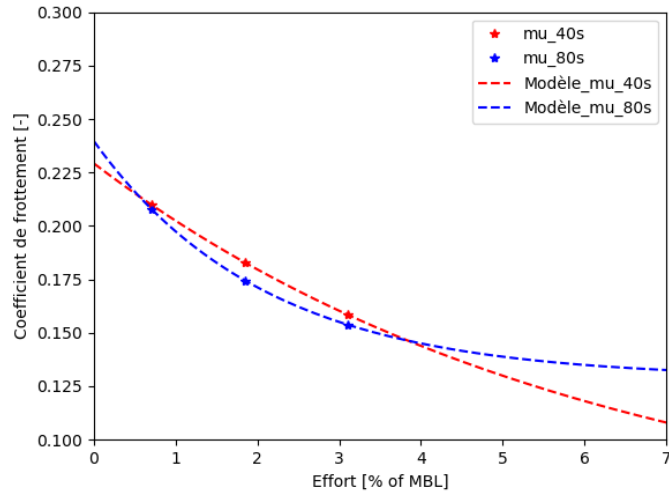


and $\mu_t \approx 0,17$



Characterization of one parameter: the friction coefficient

Article: C. Bain et al. *Experimental evaluation of the main parameters influencing friction between polyamide fibers and influence of friction on the abrasion resistance*

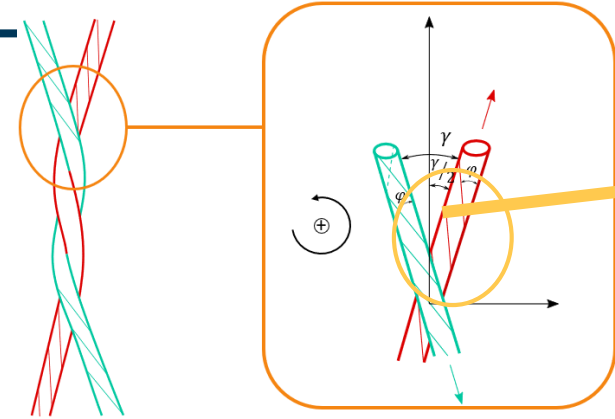


$$\mu(F) = ae^{-bF} + c$$

$$\mu(\gamma) = a \tan^{-1}(b\gamma - c) + d$$

The inter-fibers angle δ and the friction angle β have been determined as the most important parameters controlling the friction coefficient for polyamide fibers.

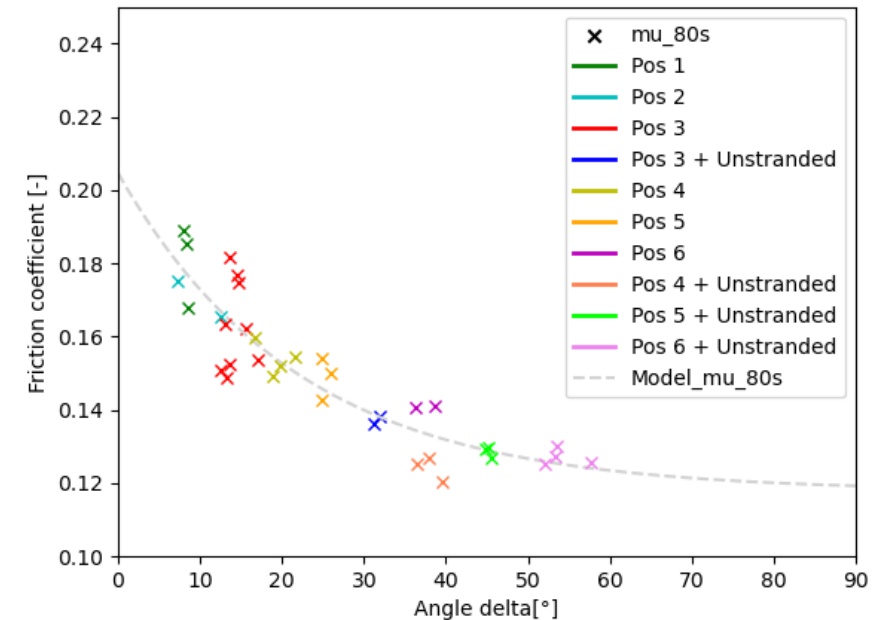
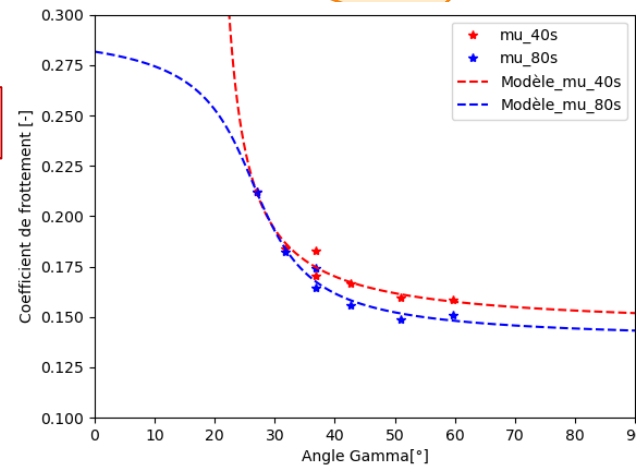
The link could be explained by the angle between the yarns



Scheme of the angle between fibres

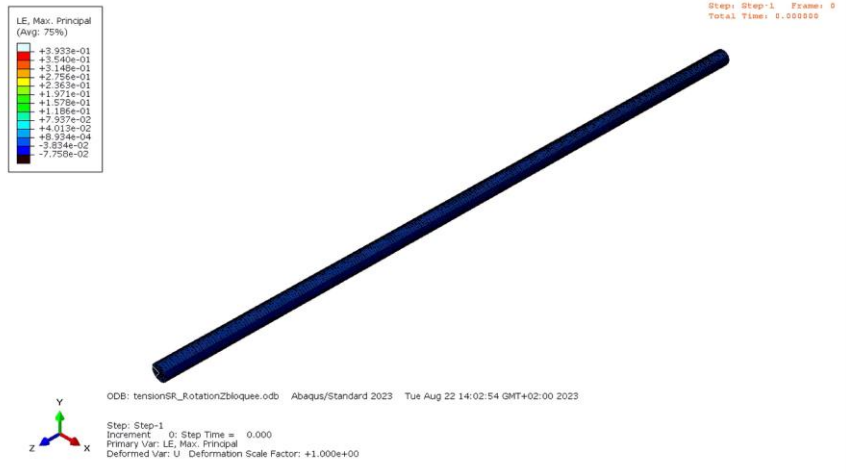
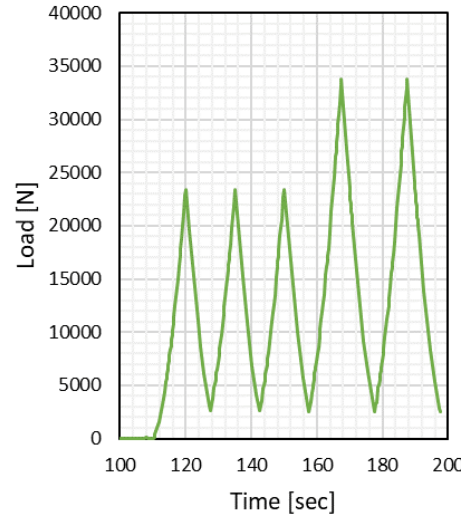
$$\delta = \gamma - 2\phi$$

$$\mu(\delta) = ae^{-b\delta} + c$$

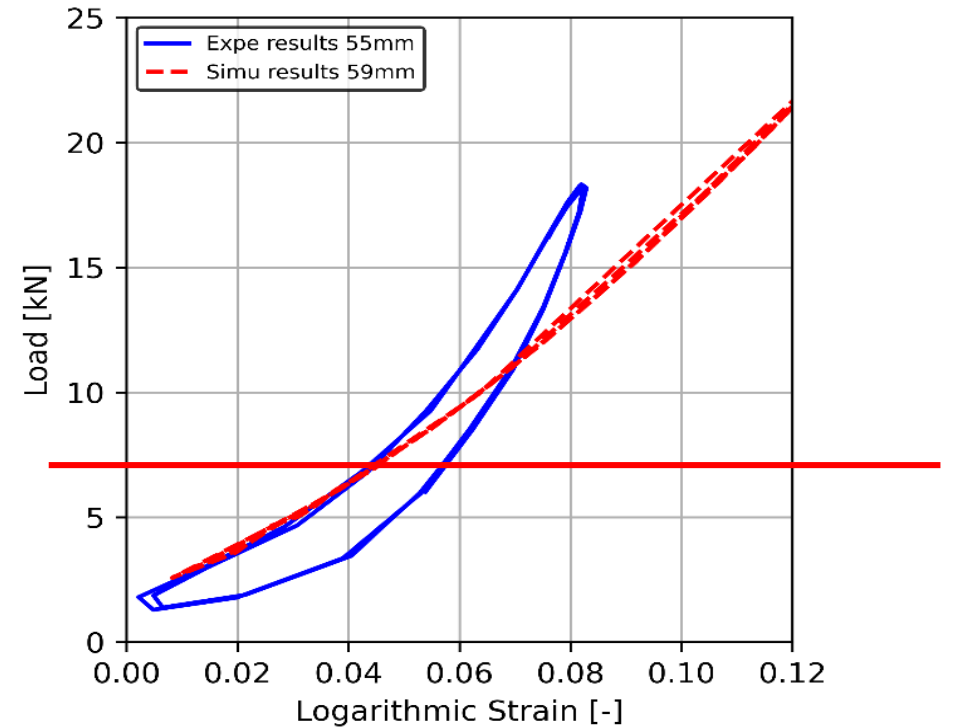


First simulation of a sub-rope using the FiBuLa law

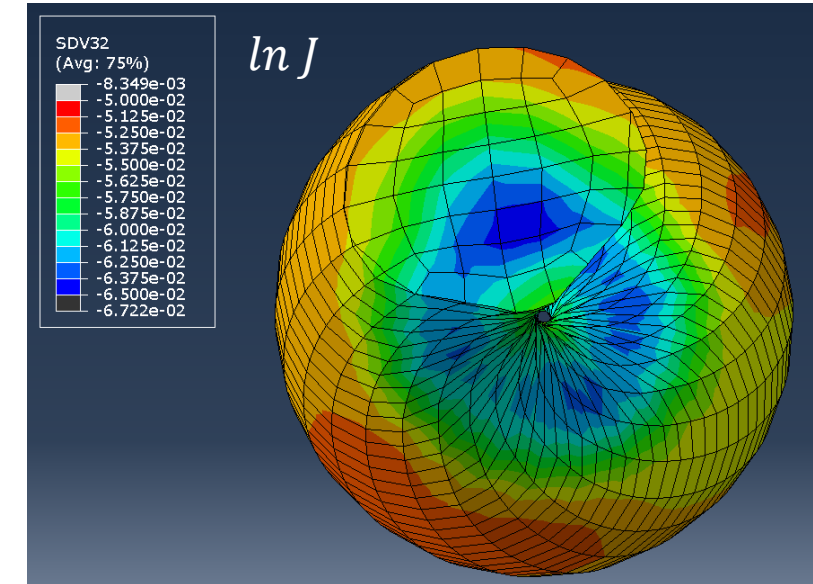
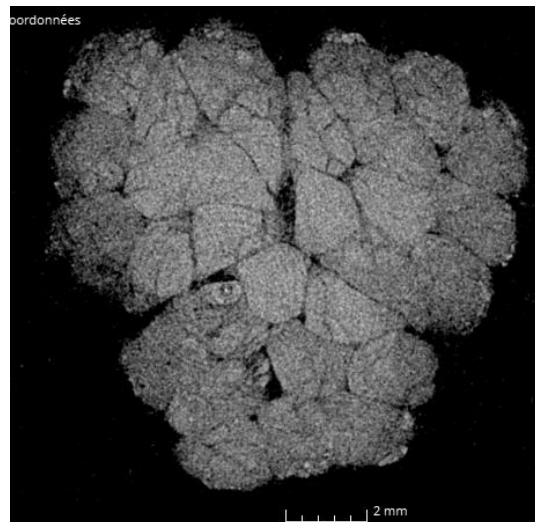
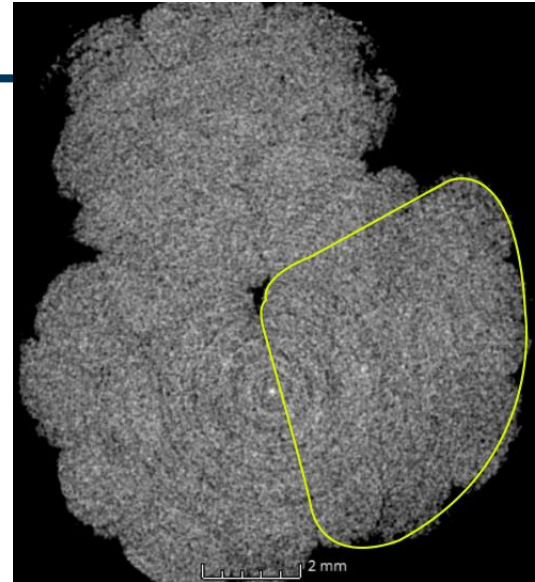
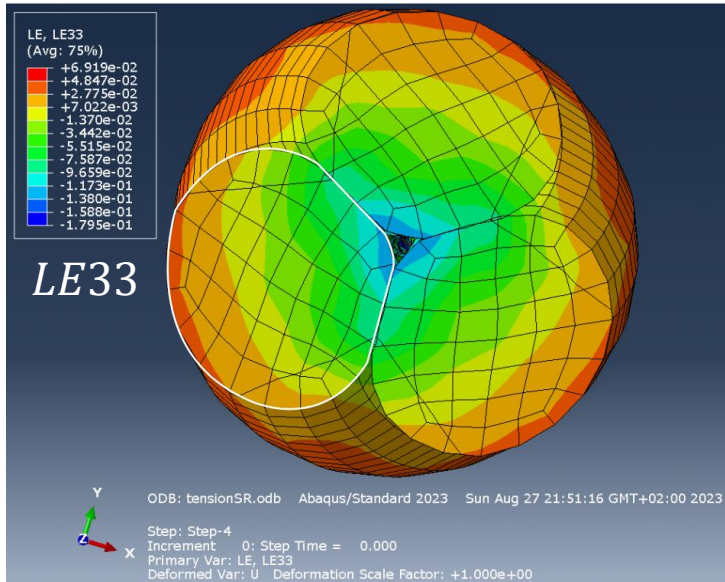
- Abaqus-Standard dynamic implicit analysis with option “quasi-static”
- Friction coefficient between strands: 0.15 (chosen using work Bain *et al.* 2022.)
- Cyclic loading (simulation duration: around 1 day)
- First comparison with experimental results



In service mean loading

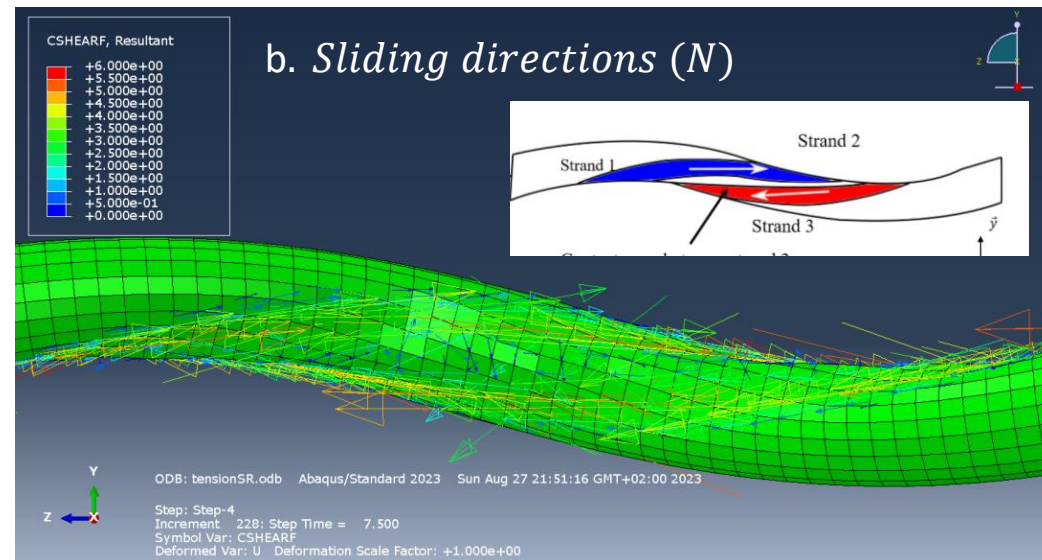
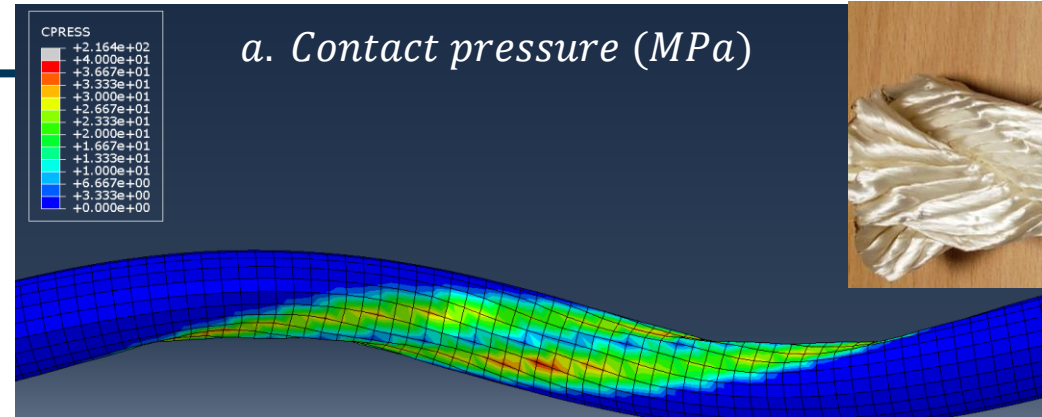
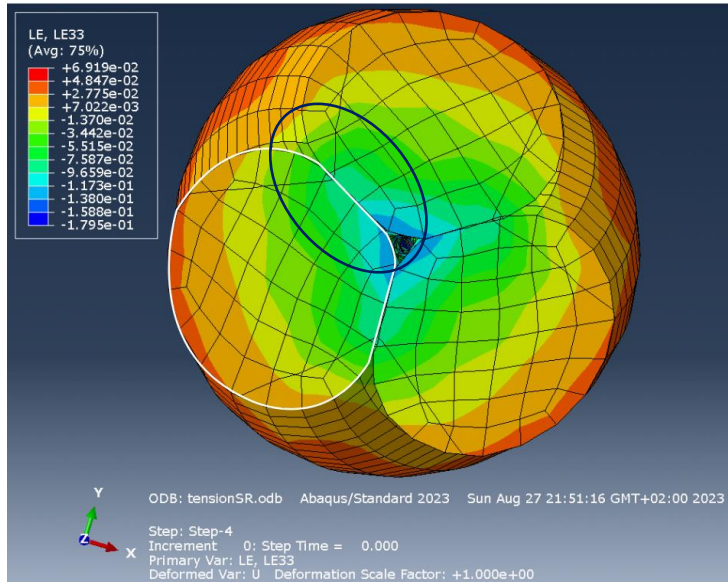


- The model is realistic though it underestimates the stiffness above 0.04 strain.
- No visible hysteresis on the model due to the friction between strands

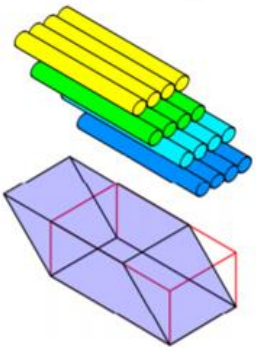
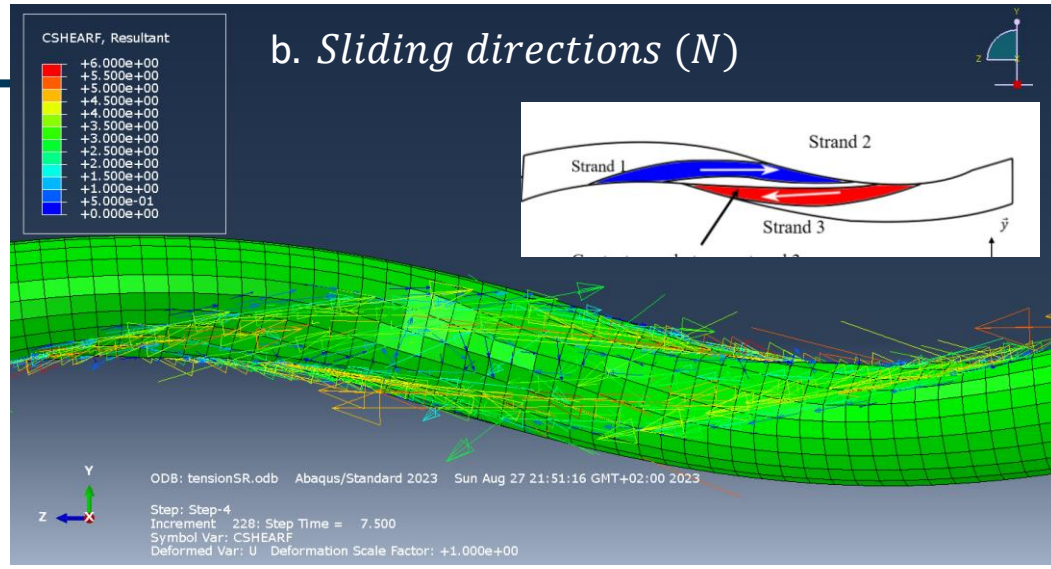


✓ Strong similarities between simulation and experimental shapes

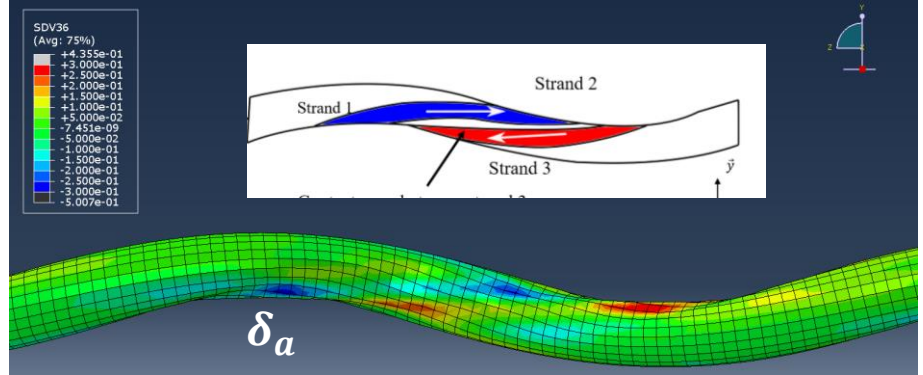
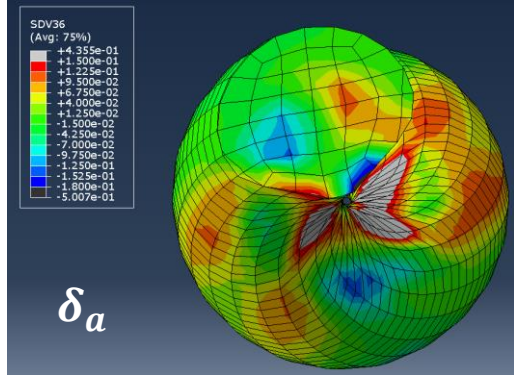
✓ Rope-yarns subjected to more compression at the inner part of the sub-rope



✓ The pressure and shear at the contact can be studied



$$\tilde{\varepsilon}_{\delta} = \begin{bmatrix} 0 & 0 & \delta_a/2 \\ 0 & 0 & \delta_b/2 \\ \delta_a/2 & \delta_b/2 & 0 \end{bmatrix}$$



✓ δ_a induced by the contact with the other strands : same directions as the sliding directions of the strands obtained with Abaqus outputs

Conclusion on the MONAMOOR project

- Development of the FiBuLa law: adaptation of A.Charmetant model to a 3-stranded polyamide sub-rope
- Development of original experimental set-ups for the experimental identifications of the parameters
- Implementation in a FORTRAN UMAT for the first calculation on Abaqus software
- First simulation of a sub-rope:
 - At the strands scale: obtention of the geometries, contact forces and sliding directions
 - At the rope-yarns scale: coherent prediction of the strain fields and new insights

→ The model is a precious tool to understand the mechanics of rope

→ The model could allow to separate the dissipation due to friction from the dissipation due to the material

Development of a meso-scale model

- Addition of the POLYAMOOD 1D law to the meso-scale model, identified on rope-yarns (instead of the current 1D elastic law)
- Inclusion of friction between rope-yarns (changing the current 2D elastic law for a 2D elasto-plastic law)
- Identification and validation of the meso-scale model performed on the MONAMOOD experimental campaign and on new tests (other scales, other construction)

